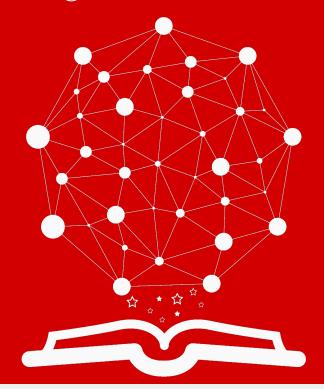
Pushing the boundaries of rational AI

through Knowledge and Reasoning



Institute of Logic and Computation

Magdalena Ortiz

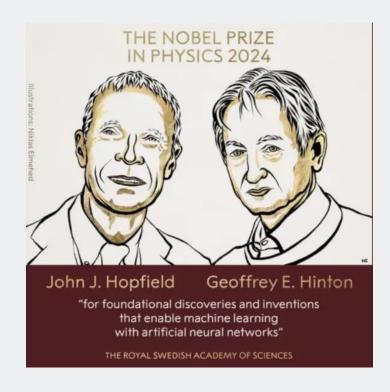
Professor for Knowledge

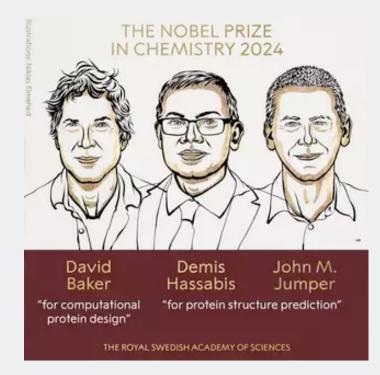
Representation and Reasoning



AI today





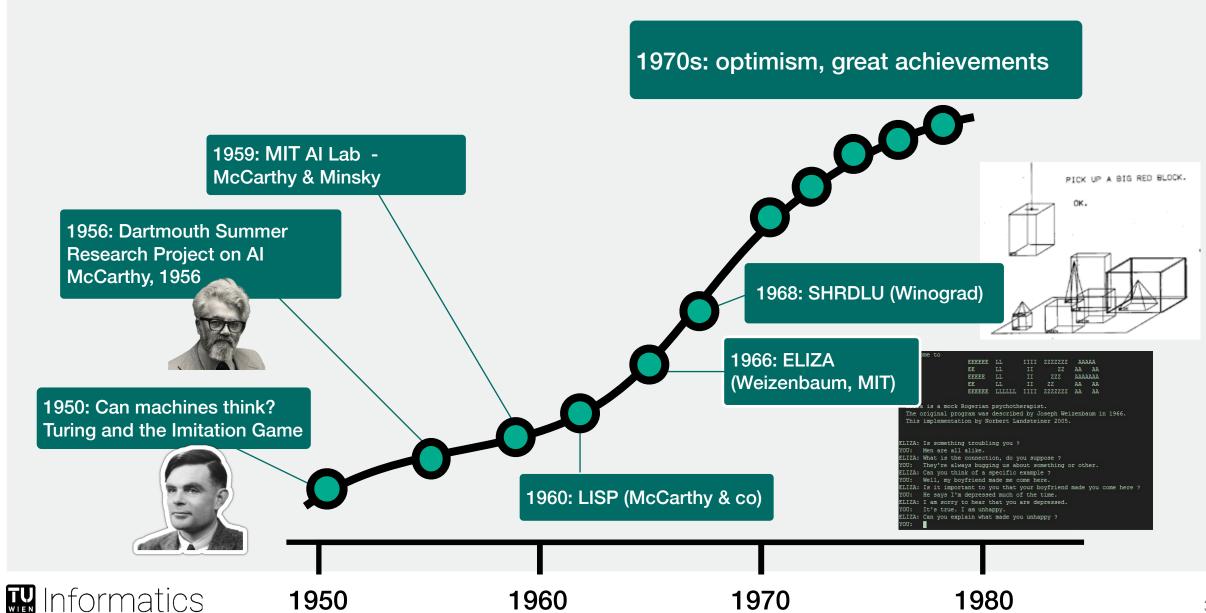


Photograph: Jonathunder Medal: Erik Lindberg



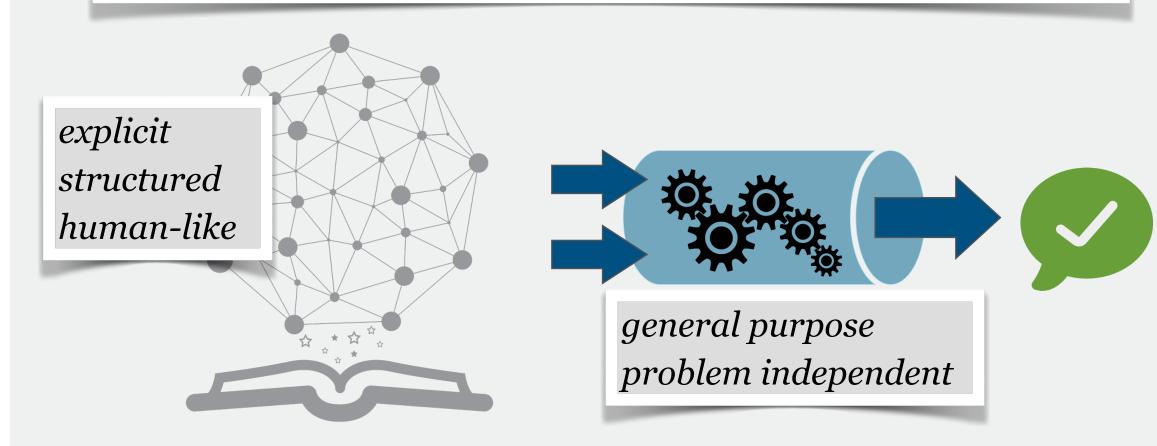


How it started



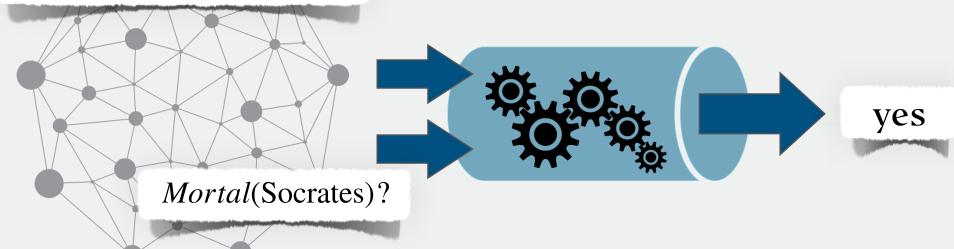
The rationality approach to AI

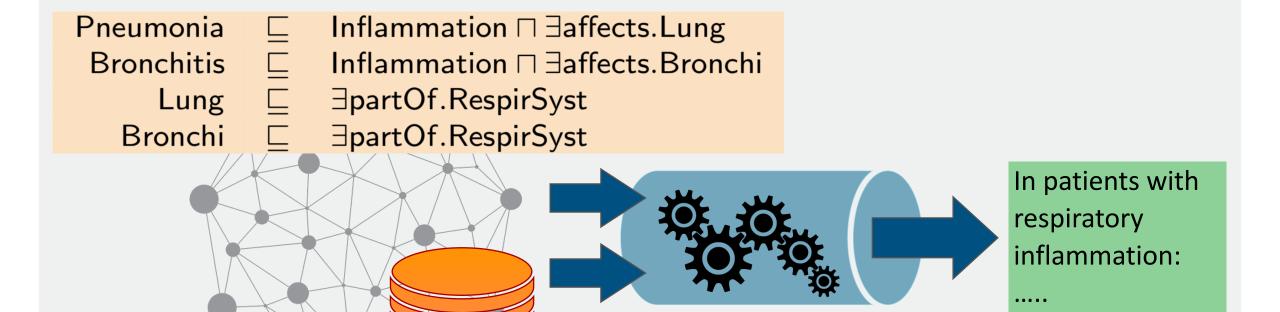
Knowledge + Reasoning ⇒ Intelligence





 $\forall x \ Person(x) \rightarrow Mortal(x)$. Person(Socrates).

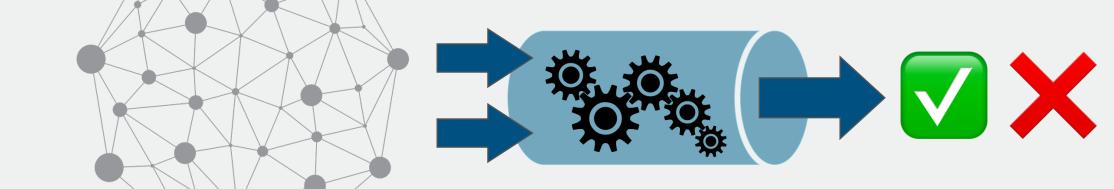




Database of patients and diagnosis



Description of a dynamic system's evolution



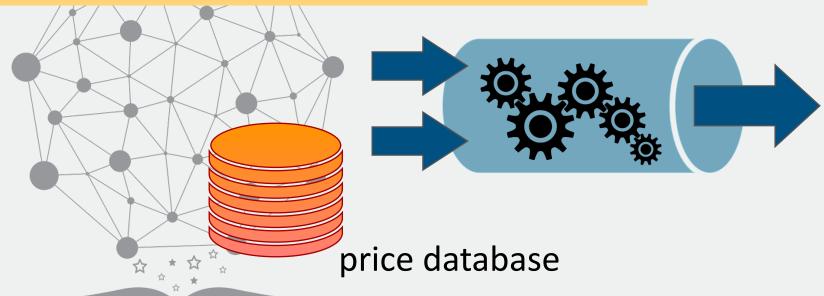
Safety conditions





All bikes have 1 frame and 2 wheels of the same type. Frame A is compatible with wheel models 1 and 3.

Frame B is compatible with wheel model 2.

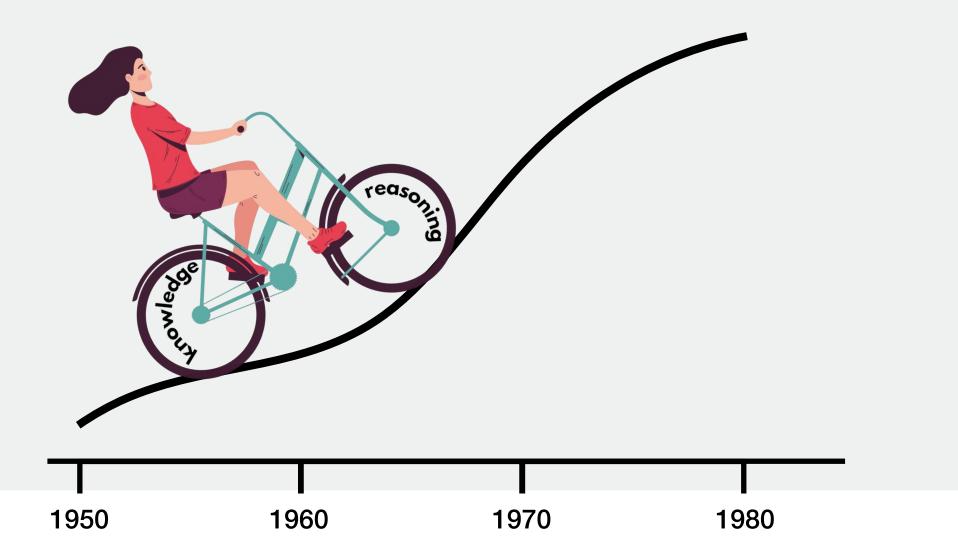


Cheapest bike configuration

...compatible with handle C and a seat of supplier X.

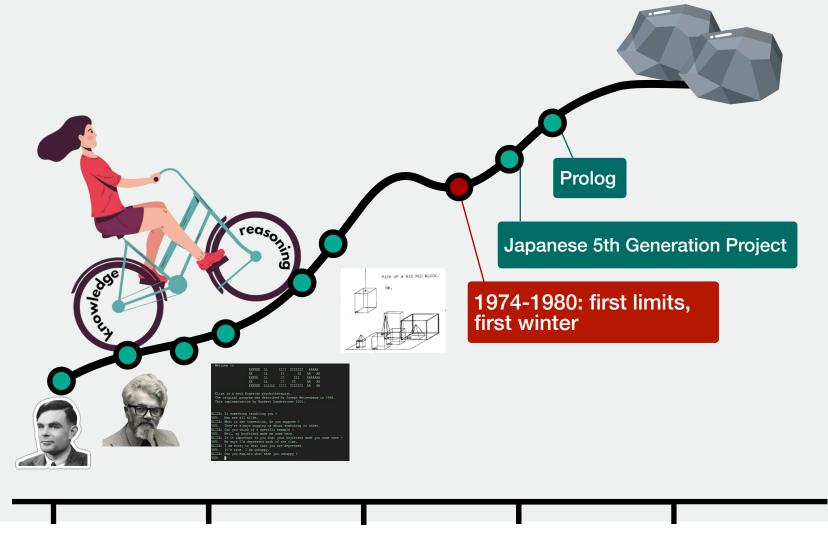


Rationality approach to AI





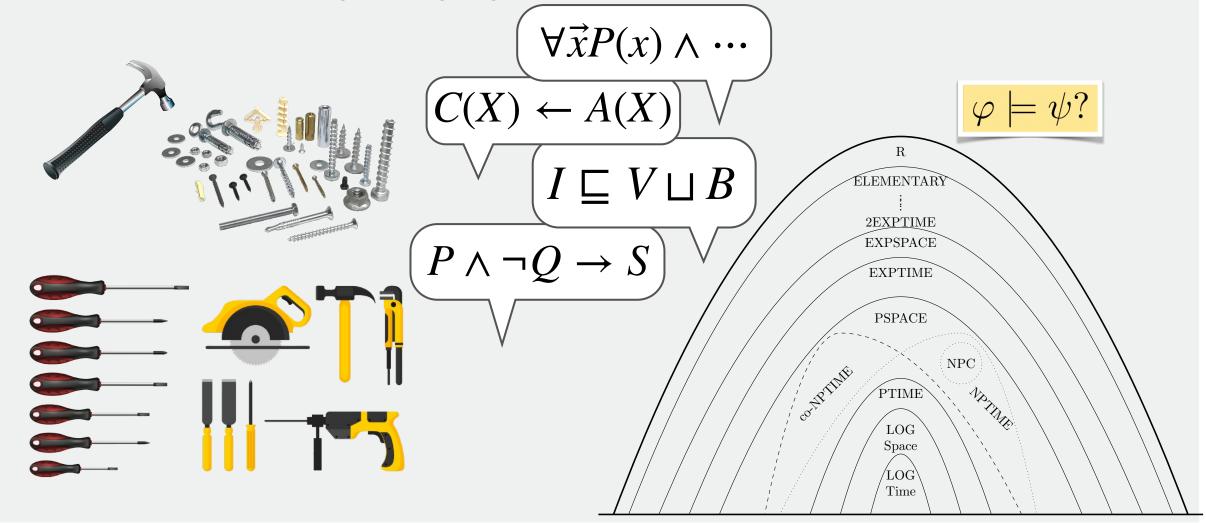
It had a good run!





High-precision logic engineering

To each problem, the right language





A lightweight superstar

for medical and life science terminologies

Description Logics: a modular family of languages balancing cost of inference vs. expressiveness

 \mathcal{EL}

```
Pneumonia ☐ Inflammation □ ∃affects.Lung
Bronchitis ☐ Inflammation □ ∃affects.Bronchi
Lung ☐ ∃partOf.RespirSyst
Bronchi ☐ ∃partOf.RespirSyst
```

polynomial reasoning!

- SNOMED CT >350,000 clinical terms, multilingual, >80 countries
- 1000s of ontologies, 1000000s of biomedical concepts
 BioPortal, OBO Foundry, NCI thesauri, WHO classifications, ICH (pharmaceutic regulation)...



The case of Guardedness

Tailoring elegant fragments

$$\exists \vec{x} (A(\vec{x}) \land \varphi(\vec{x})) \qquad \forall \vec{x} (A(\vec{x}) \to \varphi(\vec{x}))$$

- beautiful model theory
- admits elegant tools (e.g. tree automata)
- computationally robust
- excellent for describing structured domains and their evolution
 - modal logics, description logics, dynamic and temporal logics...

but terrible for asking database questions!



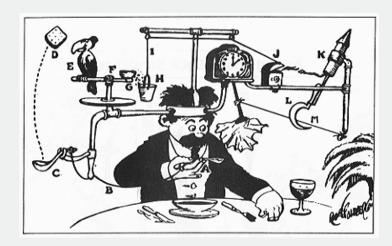


Combining languages

```
MATCH (n:Inflammation) - [:AFFECTS] -> (b:Organ) (b:) - [:PART-OF] +-> (c:RespSystem) WHERE n.type = 'Chronic' RETURN n; q(\vec{x}) \leftarrow \exists \vec{y} \; \rho_1(\vec{x_1}) \land \cdots \land \rho_n(\vec{x_n}) \\ \rho ::= R \mid \rho \cdot \rho \mid \rho \cup \rho \mid \rho^*
```

inherently different from languages for describing structured knowledge

$$\varphi \models \psi$$



Rube Goldberg (published Collier's, Sept 1931)

Pneumonia \sqsubseteq Inflammation $\sqcap \exists$ affects.Lung Bronchitis \sqsubseteq Inflammation $\sqcap \exists$ affects.Bronchi

 $\mathsf{Lung} \quad \sqsubseteq \quad \exists \mathsf{partOf.RespirSyst}$

Bronchi $\sqsubseteq \exists partOf.RespirSyst$

$$\exists \vec{x} (A(\vec{x}) \land \varphi(\vec{x})) \qquad \forall \vec{x} (A(\vec{x}) \to \varphi(\vec{x}))$$



Not for the faint hearted!

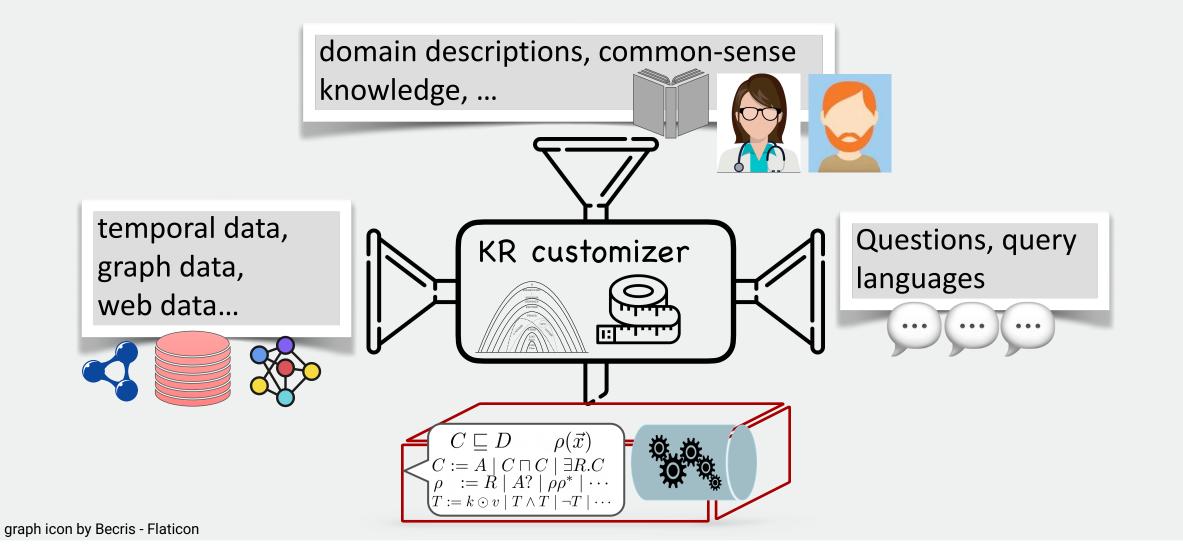
$$\varphi := \exists \vec{x} (A(\vec{x}) \land \varphi(\vec{x})) \qquad \psi := q(\vec{x}) \leftarrow \exists \vec{y} \ \rho_1(\vec{x_1}) \land \cdots \land \rho_n(\vec{x_n})$$
$$\forall \vec{x} (A(\vec{x}) \rightarrow \varphi(\vec{x})) \qquad \rho ::= R \mid \rho \cdot \rho \mid \rho \cup \rho \mid \rho^*$$



tombstone by Freepik

	IQs		CQs		2RPQs		C2RPQs	
	Data	Combined	Data	Combined	Data	Combined	Data	Combined
	complexity	complexity	complexity	complexity	complexity	complexity	complexity	complexity
$\operatorname{DL-Lite} \operatorname{DL-Lite}_{\mathcal{R}}$	in AC ₀	NLogSpace	in AC ₀	NP	NLogSpace	P	NLogSpace	PSPACE
$\mathcal{EL},\mathcal{ELH}$	P	P	P	NP	P	P	P	PSPACE
\mathcal{ELI} , \mathcal{ELHI}_{\perp} , Horn- \mathcal{SHOIQ}	P	Exp	P	Exp	P	Exp	P	Exp
ALC, ALCHQ	coNP	EXP	coNP	EXP	coNP	EXP	coNP-hard	2Exp
ALCI, SH, SHIQ	coNP	EXP	coNP	2Exp	coNP	Exp	coNP-hard	2Exp
SHOIQ	coNP-hard	coNExp	coNP-hard	coN2 Exp-hard ^a	coNP-hard	coNExp	coNP-hard	coN2 Exp-hard ^b

Rightsizing on demand





Some semantic challenges



All trains to the airport depart form platform 1.

All ingredients are

GOURMET WOOD FIRED PIZZAS

Alla Puttanesca Tomato, chilli, capers, black olives,

mozzarella and oregano

Alla Margherita Tomato, bocconcini, parmesan, mozzarella and fresh basil

Prosciutto Cotto e Funghi Prosciutto ham, field mushrooms, tomato, mozzarella and oregano

$$\not\models \forall x \; (train(x) \land goesTo(x, airport)) \rightarrow departPlatform(x, 1)$$



All buyers are happy and recommend the product?

 $\not\models \forall x \ buyer(x) \rightarrow recommends(x, product)$



An unachiavable dream?

Dozens of works since the 1980s, but it is hard!

		ALC	ALCQO	\mathcal{ALCI}	\mathcal{ALCIO}	
Concept circ.	$\#M \le n, \#F \le n$	NP^{NExp}				
	(unrestricted)	NExp^{NP} even if $\prec = \emptyset$, and either TBox= \emptyset or ABox= \emptyset				
Minim. roles	$\mathrm{TBox} = \emptyset$	NExp ^{NP} even	if $\#M \le 1, \#F \le 0$	Unde	cidable	
	$TBox \neq \emptyset$	Undecidable				
Fixed roles		Highly undecidable , even if $TBox = \emptyset$, $\prec = \emptyset$				

The Complexity of Circumscription in DLs (Bonatti, Lutz, & Wolter 2009)

With hard work and advanced techniques, feasible approaches to non-monotonicity

	Pointwise Circumscription				
	basic	general			
$DL ext{-Lite}^\mathcal{H}$	≤ P	NP-c*	≤ NExp [†]		
$DL ext{-Lite}_{horn}^{\mathcal{H}}$	≥ NP	≥ NP	< NExp [†]		
extstyle ext	$\geq \Sigma_2^p$	$\geq \Sigma_2^p$	\leq NExp †		

Bonatti, Di Stefano, O., Šimkus (2023)

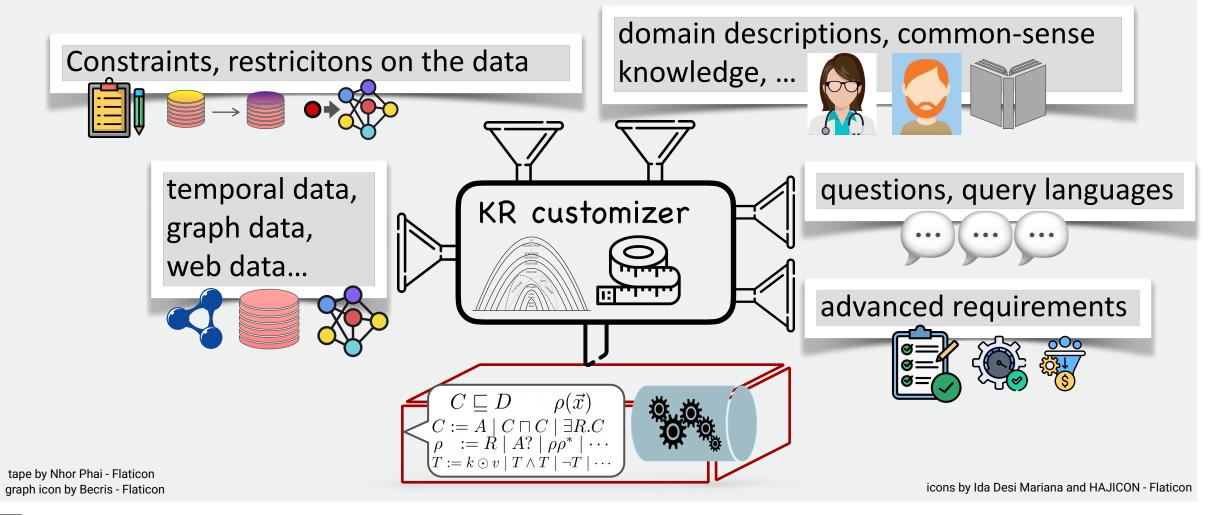
Theorem: Answering safe-range queries is feasible in co-NP in data complexity for *ALCHOIQ* with closed predicates.

S. Lukumbuzya, M. O and M. Šimkus (2023)



Tailoring advanced solutions

in an ever-evolving landscape





Advanced reasoning

The aims:

- correct
- optimal
- practicable

algorithms for different types of data, knowledge, constraints, queries, requirements....

explanations

- how is a conclusion derived?
- why is a desired conclusion missing?

translations among languages

- equivalent, faithful up to a vocabulary / query type...
- leveraging constraints
- absorb some components

compilations

- costly reasoning offline, efficient online access
- absorb some components

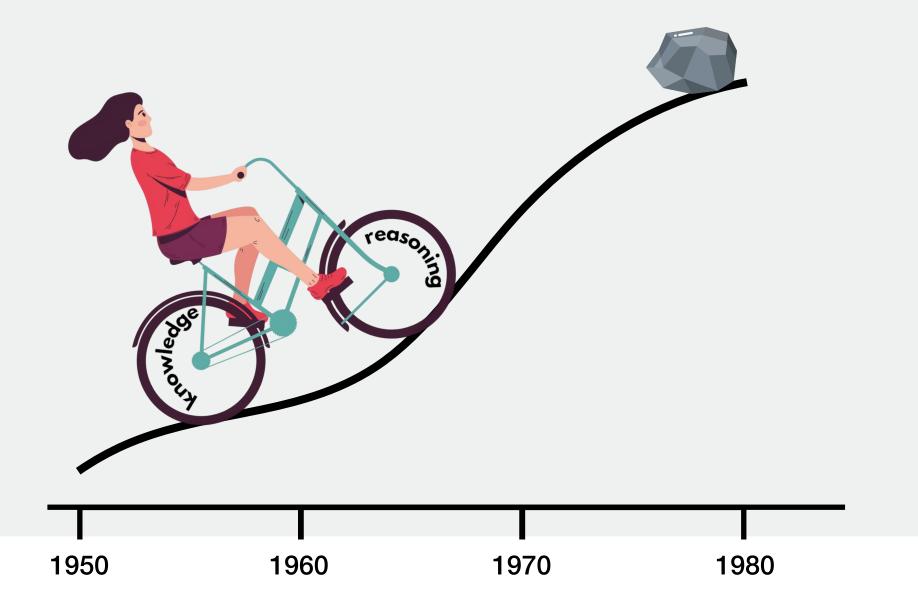
incremental reasoning

- validate changes before execution
- avoid recomputation after updates



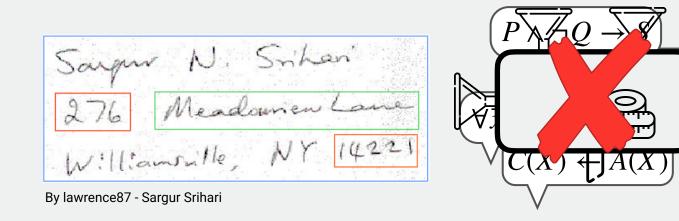


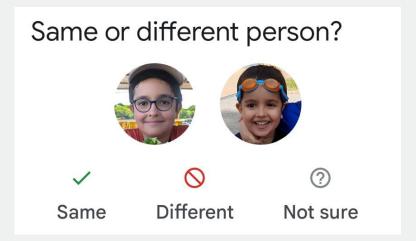
AI = Knowledge + Reasoning?





The learning-centric approach to AI

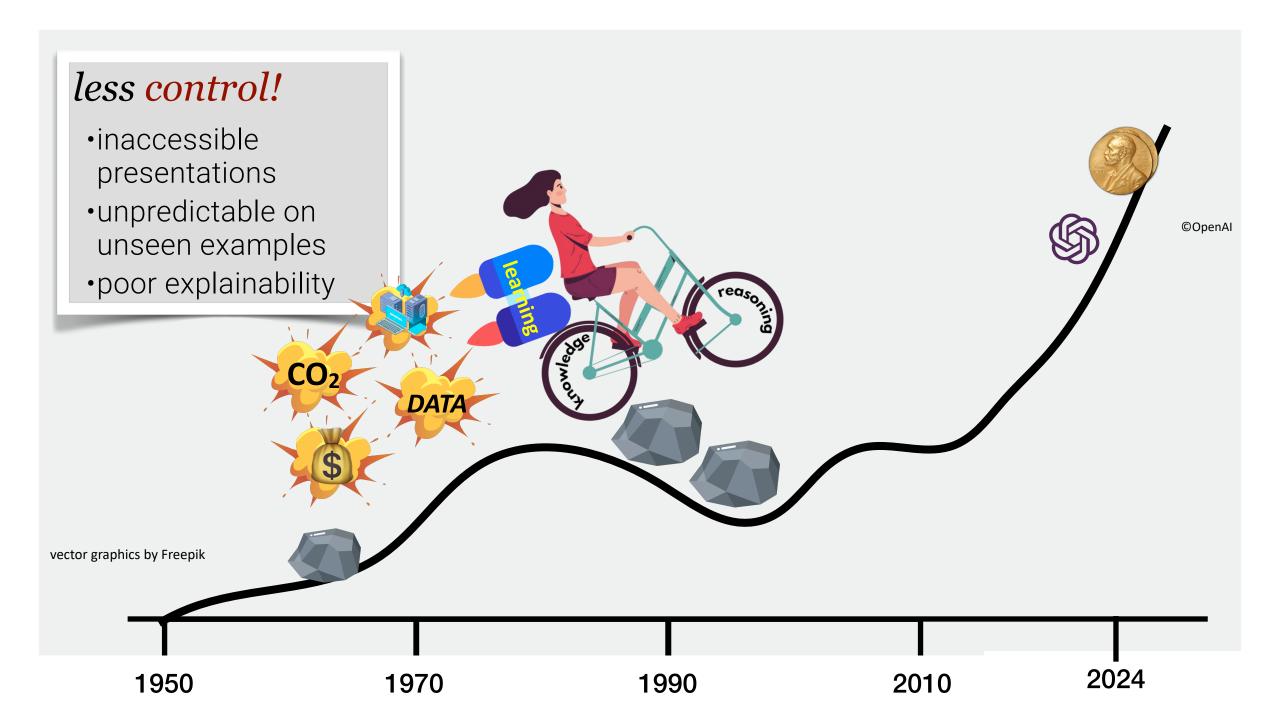




Mimic our learning rather than our reasoning

- learn to make predictions from data and examples
- improve performance over time





I hung two t-shirts to dry outside. They took one hour to dry

I have a 4liter jug and a 2 liter jug. How do I measure two liters of water?



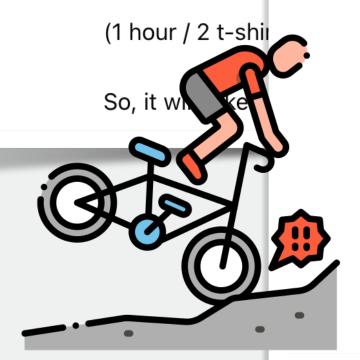
If it took one ho calculate how lo

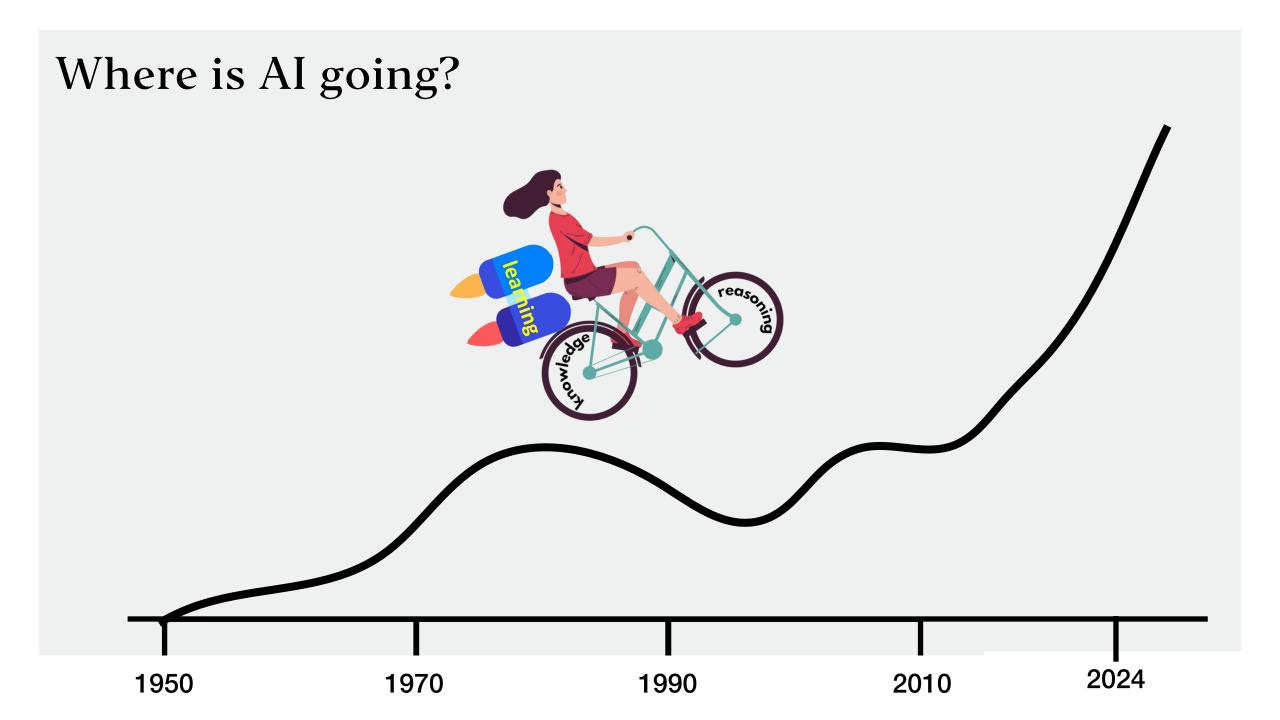


To measure exactly 2 liters of water using a 4-liter jug and a 2-liter jug, you can follow these steps:

- 1. Fill the 4-liter jug to its maximum capacity.
- 2. Pour the water from the 4-liter jug into the 2-liter jug. This will leave you with 2 liters of water in the 4-liter jug.
- 3. Now, you have 2 liters of water in the 4-liter jug, but the 2-liter jug is empty.
- 4. Fill the 4-liter jug to its maximum capacity again.
- 5. Carefully pour the water from the 4-liter jug into the 2-liter jug. Since the 2-liter jug already has 2 liters of water, it can only hold an additional 2 liters, so you'll end up with exactly 2 liters of water in the 2-liter jug.

Now you have successfully measured 2 liters of water using a 4-liter jug and a 2-liter jug.





Where is Al going?







