

Sustainable Blockchains

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Science and
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Nov. 3 2025

- Centralized (DigiCash)
one party controls everything
- Decentralized but Permissioned (Hyperledger,...)
fixed list of parties
- Fully Permissionless (Bitcoin, Chia, Ethereum,...)
everyone can participate!

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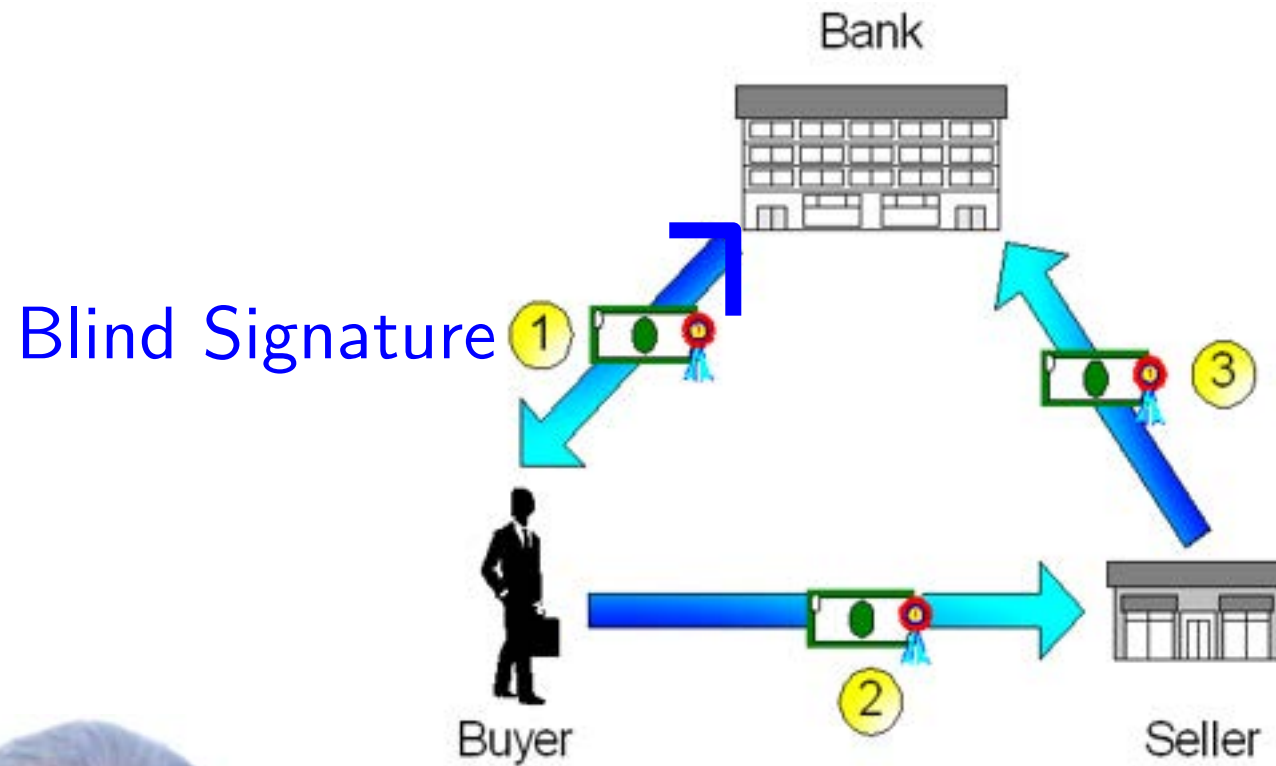
1980's Cryptography

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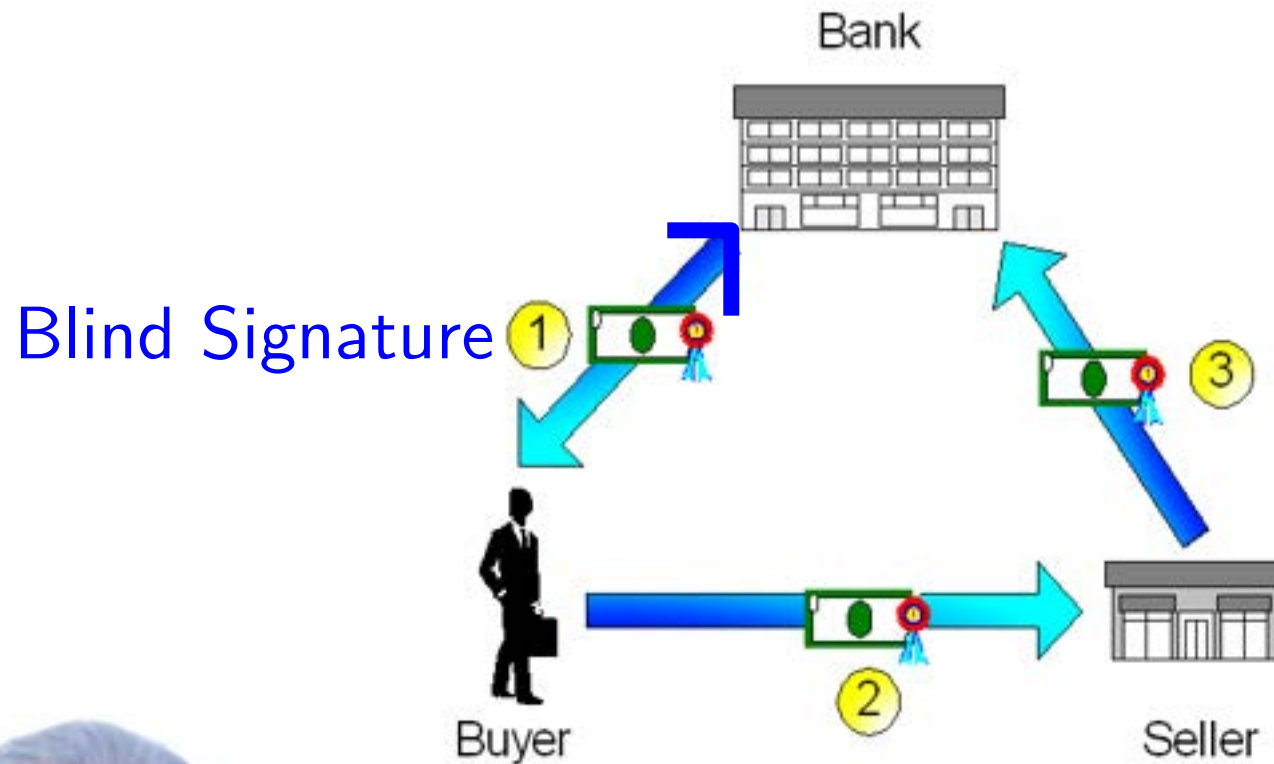
Blockchains

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(Centralized) Anonymous E-Cash, 80-90's



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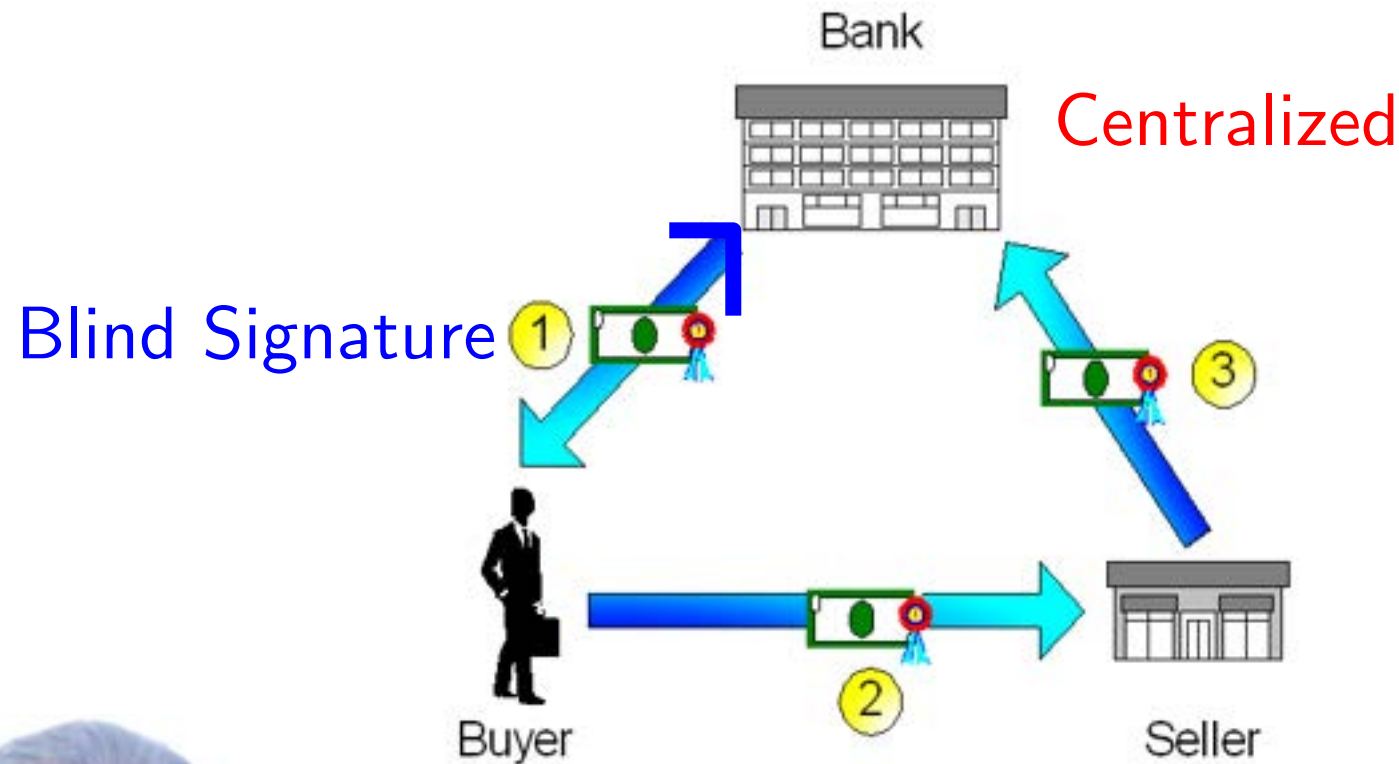
DigiCash

welcome

to the DigiCash Webserver

numbers that are money ...

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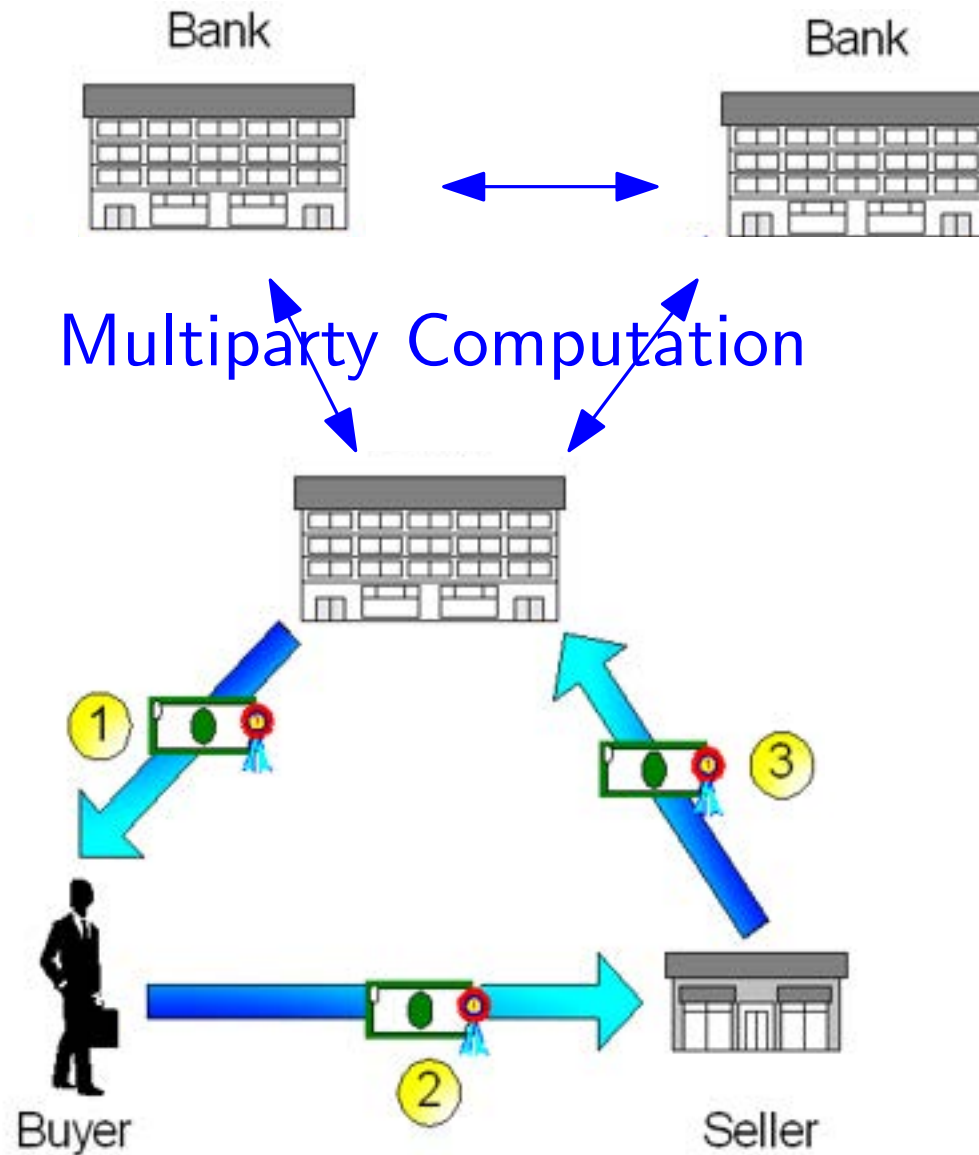
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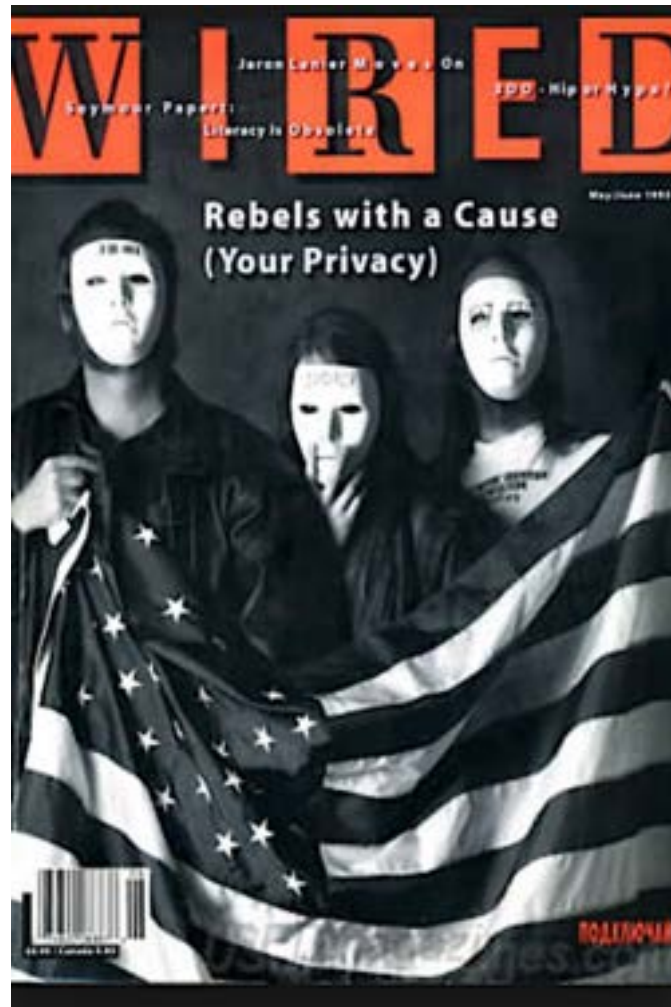
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Decentralization using 80s Crypto



<https://en.wikipedia.org/wiki/Cypherpunk>

A **cypherpunk** is any activist advocating widespread use of strong cryptography and privacy-enhancing technologies as a route to social and political change.



Permissionless E-Cash / Nov. 2008

Bitcoin: A Peer-to-Peer Electronic Cash System

Satoshi Nakamoto
satoshin@gmx.com
www.bitcoin.org

Abstract. A purely peer-to-peer version of electronic cash would allow online payments to be sent directly from one party to another without going through a financial institution. Digital signatures provide part of the solution, but the main benefits are lost if a trusted third party is still required to prevent double-spending. We propose a solution to the double-spending problem using a peer-to-peer network. The network timestamps transactions by hashing them into an ongoing chain of hash-based proof-of-work, forming a record that cannot be changed without redoing the proof-of-work. The longest chain not only serves as proof of the sequence of events witnessed, but proof that it came from the largest pool of CPU power. As long as a majority of CPU power is controlled by nodes that are not cooperating to attack the network, they'll generate the longest chain and outpace attackers. The network itself requires minimal structure. Messages are broadcast on a best effort basis, and nodes can leave and rejoin the network at will, accepting the longest proof-of-work chain as proof of what happened while they were gone.

Bitcoin Consensus

Consensus in a permissionless setting is impossible

Bitcoin Consensus

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Bitcoin Consensus

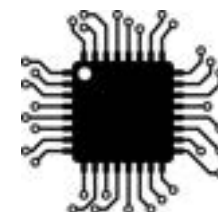
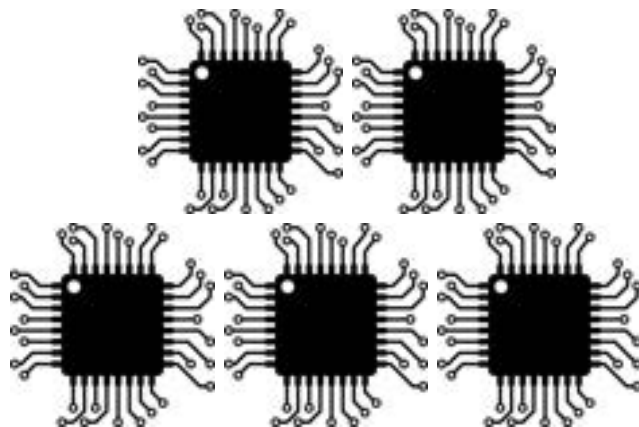
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Bitcoin Consensus

Nakamoto Consensus

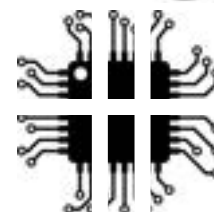
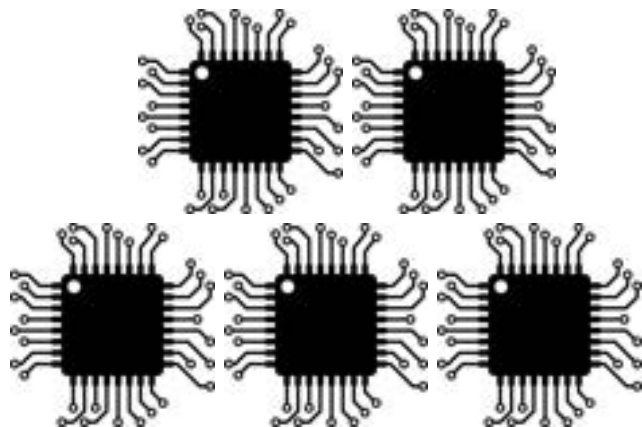
Assumption: Majority of computing power controlled by honest parties



Bitcoin Consensus

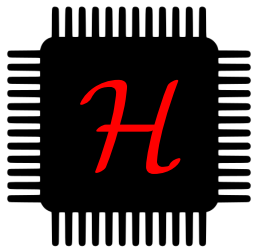
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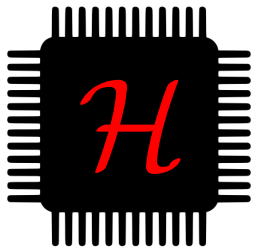
Proofs of Work [DworkNaor92]

How can  prove that it evaluated $\mathcal{H}$ 10^9 times?



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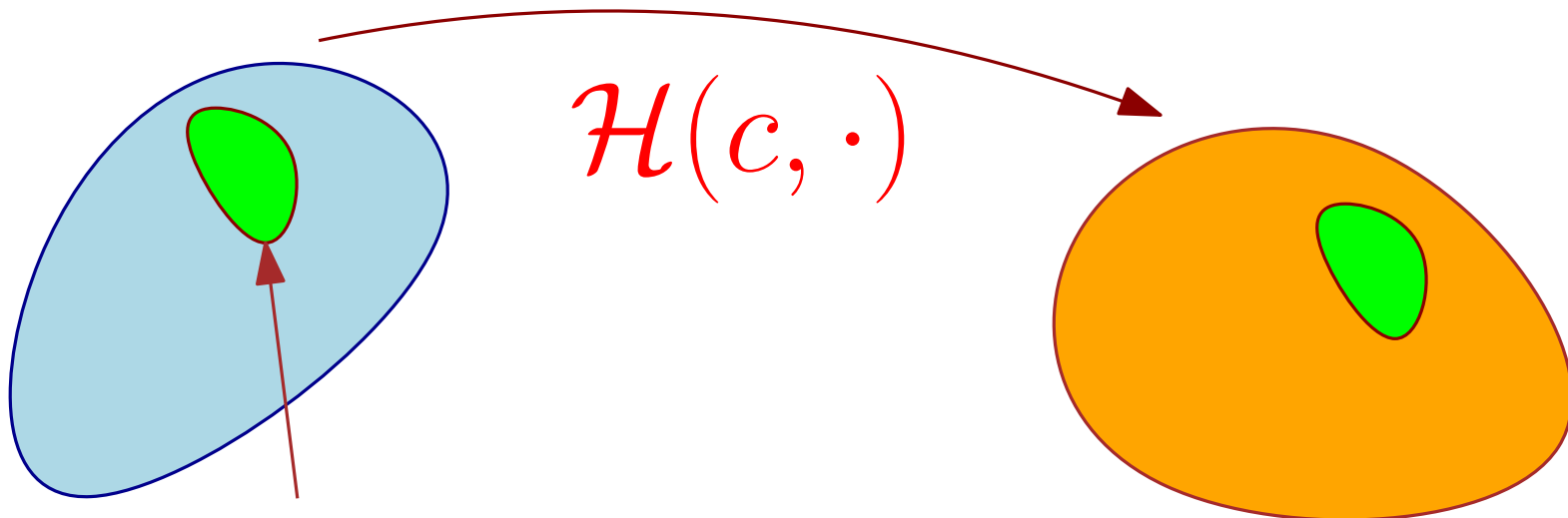
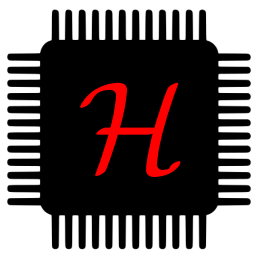


$$\begin{array}{c} \mathcal{H}(1) \\ \mathcal{H}(2) \\ \hline \mathcal{H}(3) \\ \vdots \\ \mathcal{H}(1000000000) \end{array} \rightarrow$$



Proofs of Work [DworkNaor92]

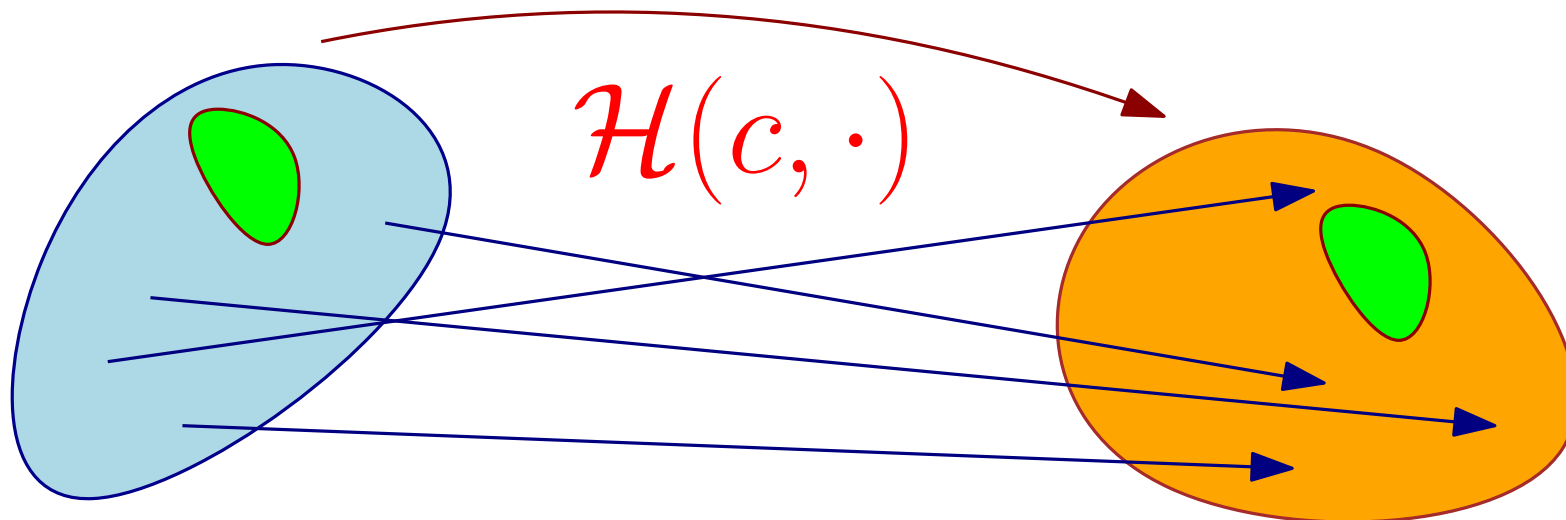
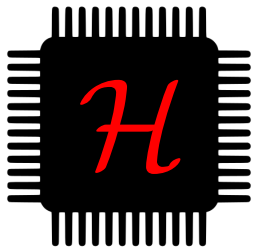
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$$\{X : \mathcal{H}(c, X) = 000000000 \dots\}$$

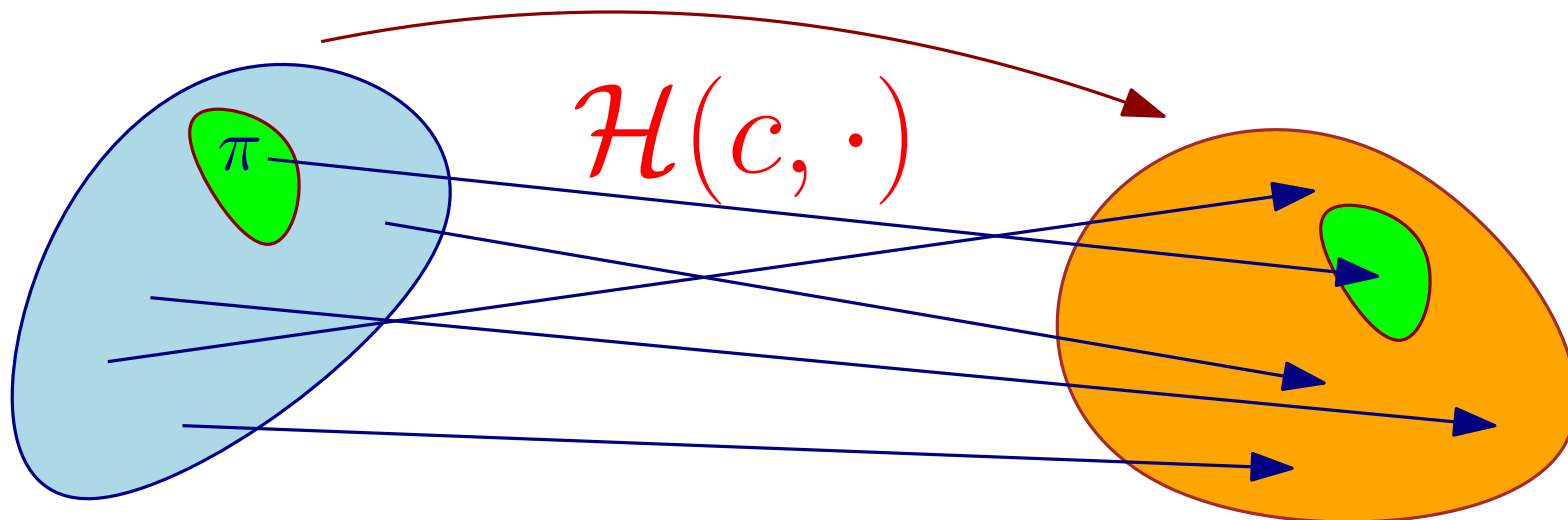
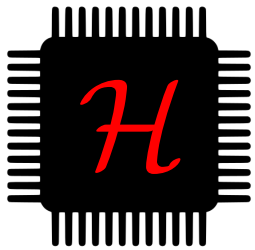
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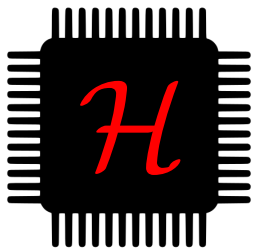
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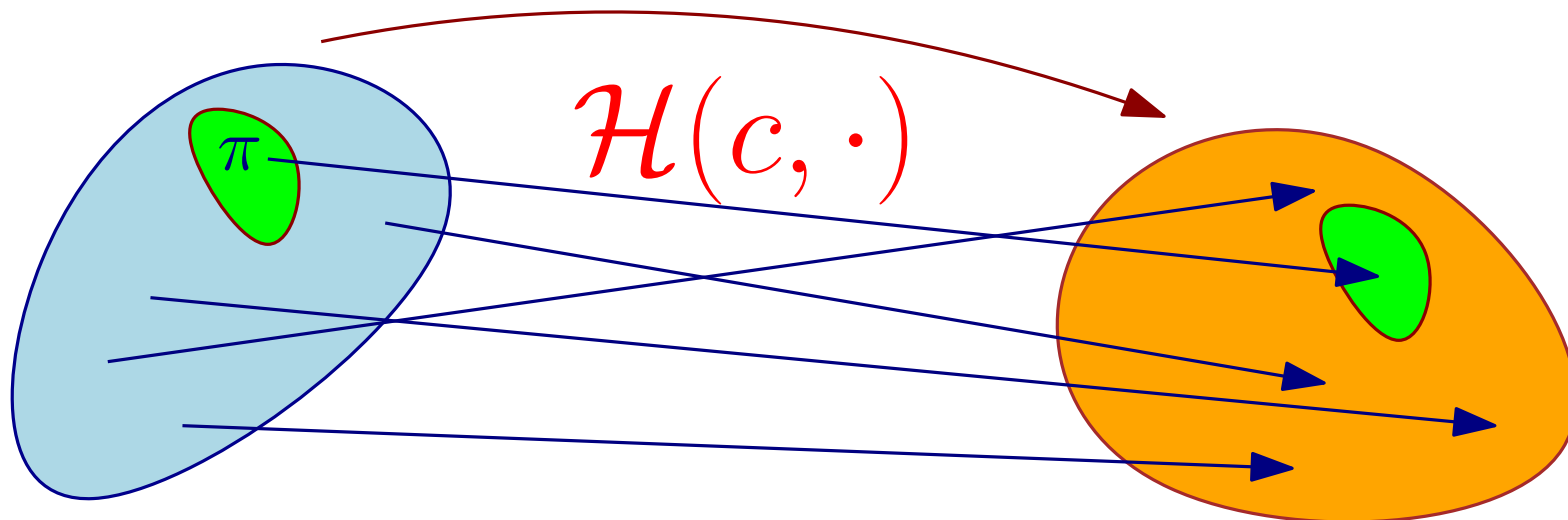
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π

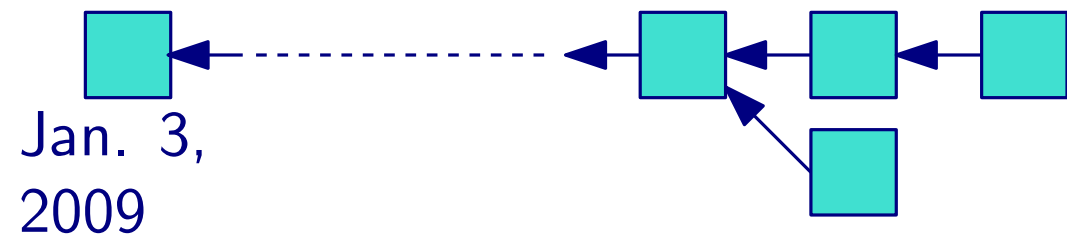
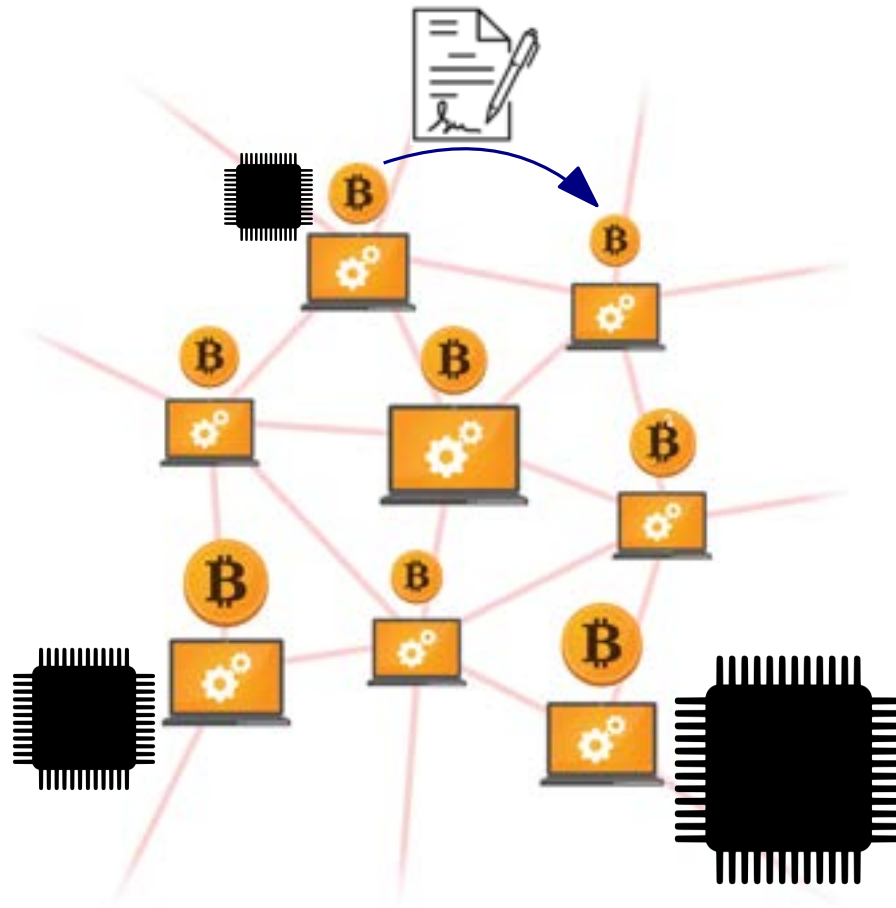


$$\mathcal{H}(c, \pi) \stackrel{?}{=} 0000000000 \star \star \star \star$$

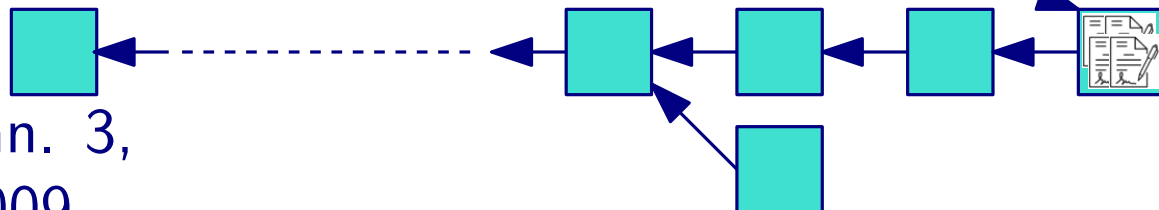
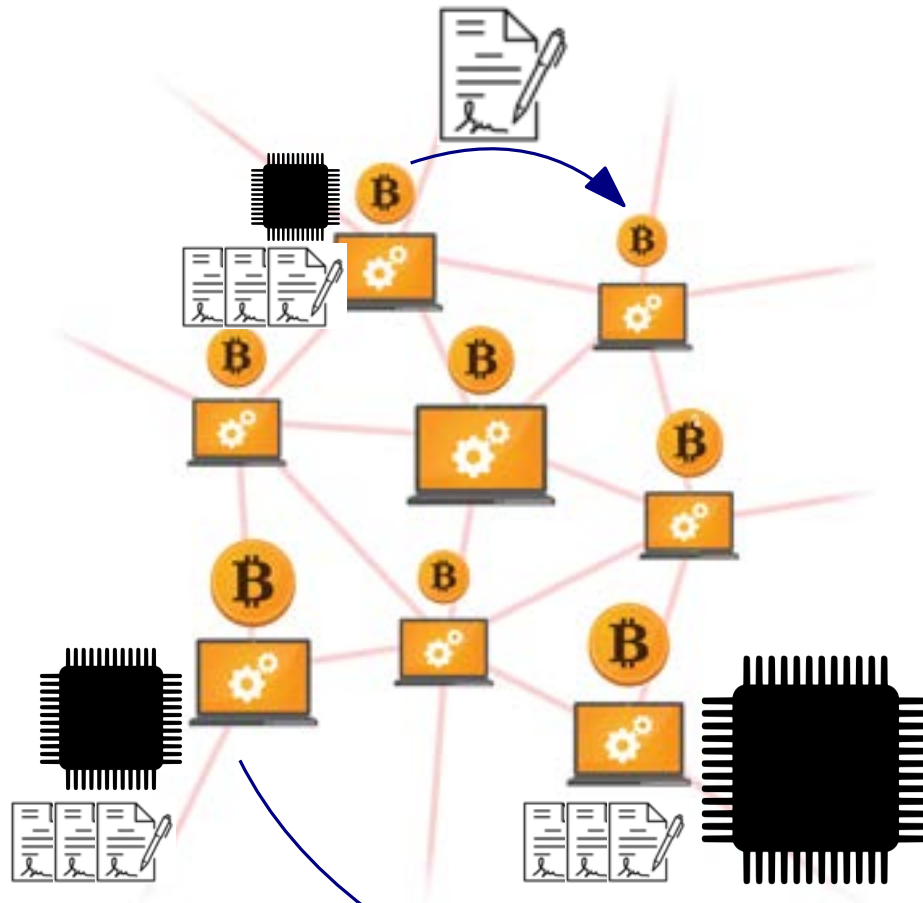


10^9 required in expectation to find a proof π

Proofs of Work in Bitcoin



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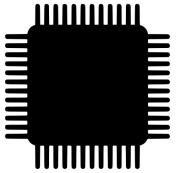
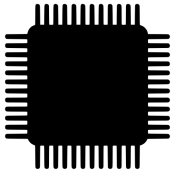


Jan. 3,
2009

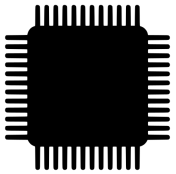
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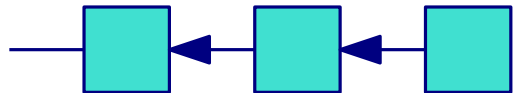
τ



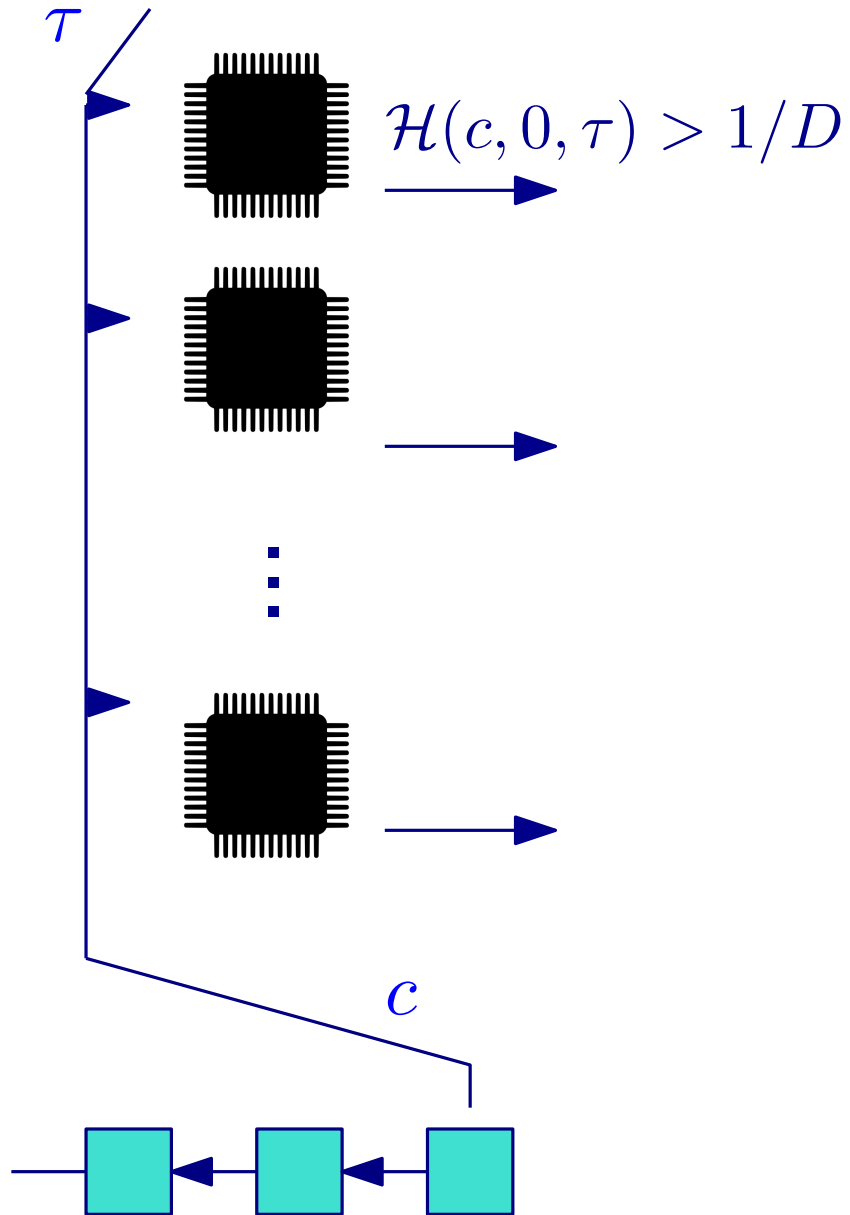
⋮



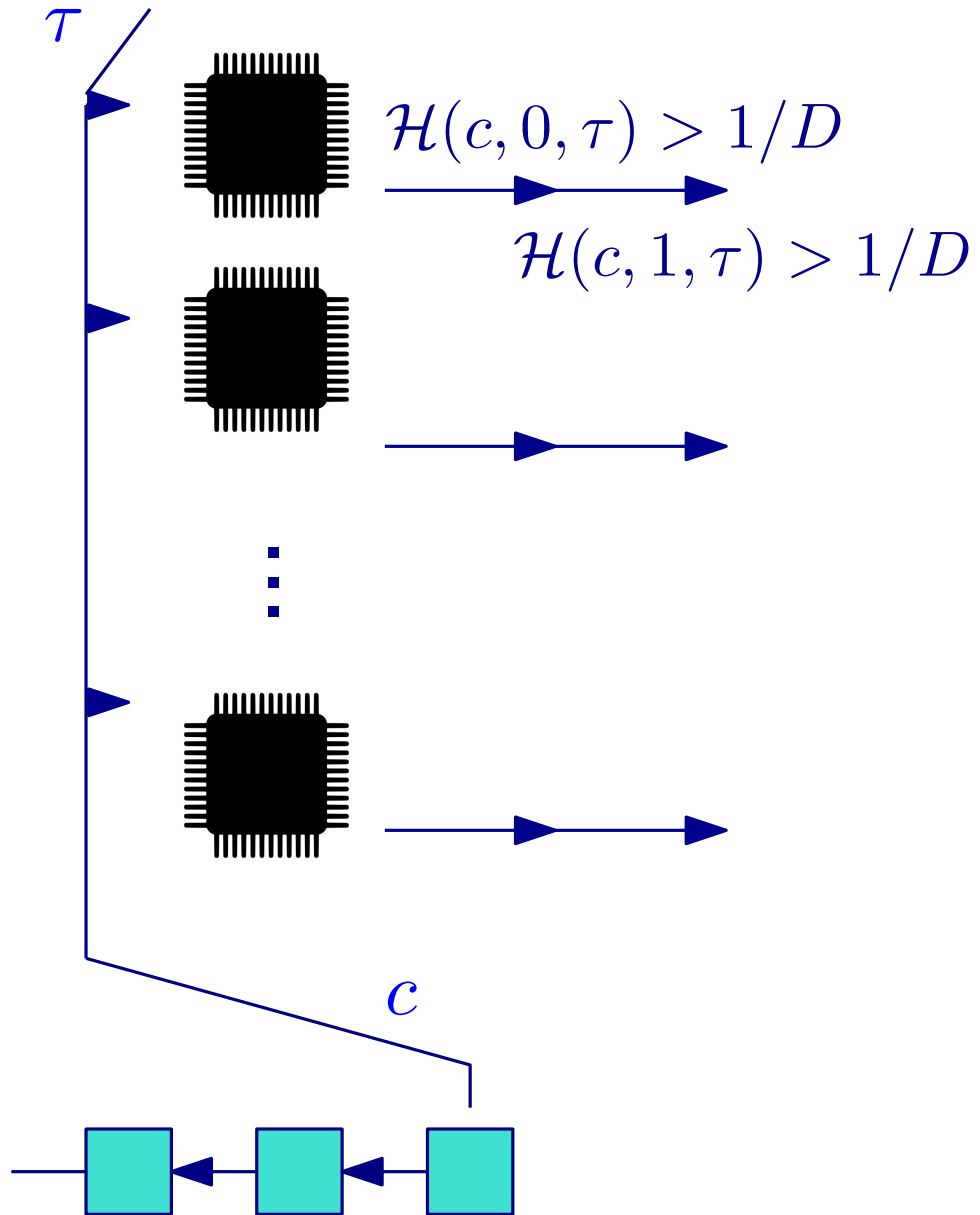
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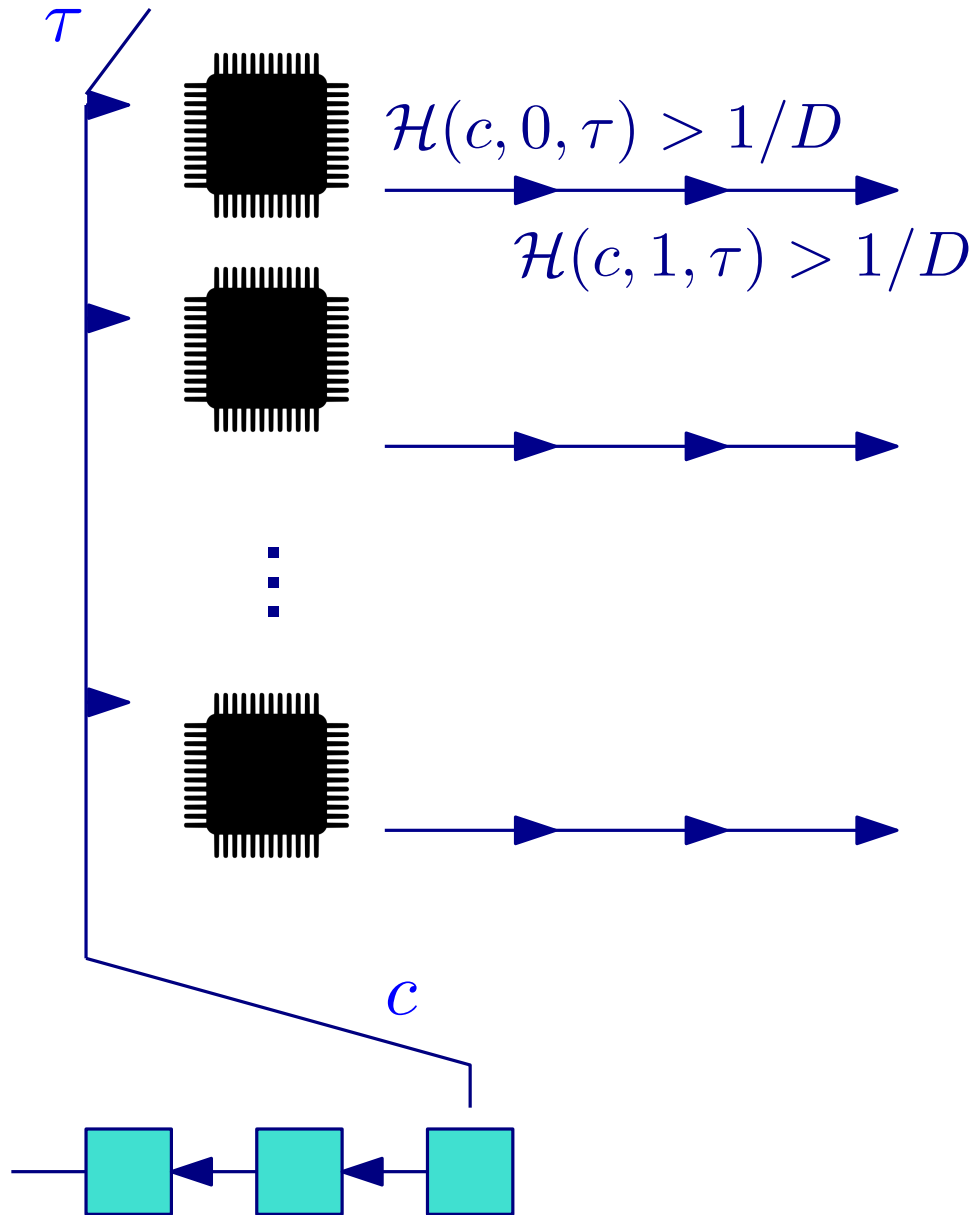
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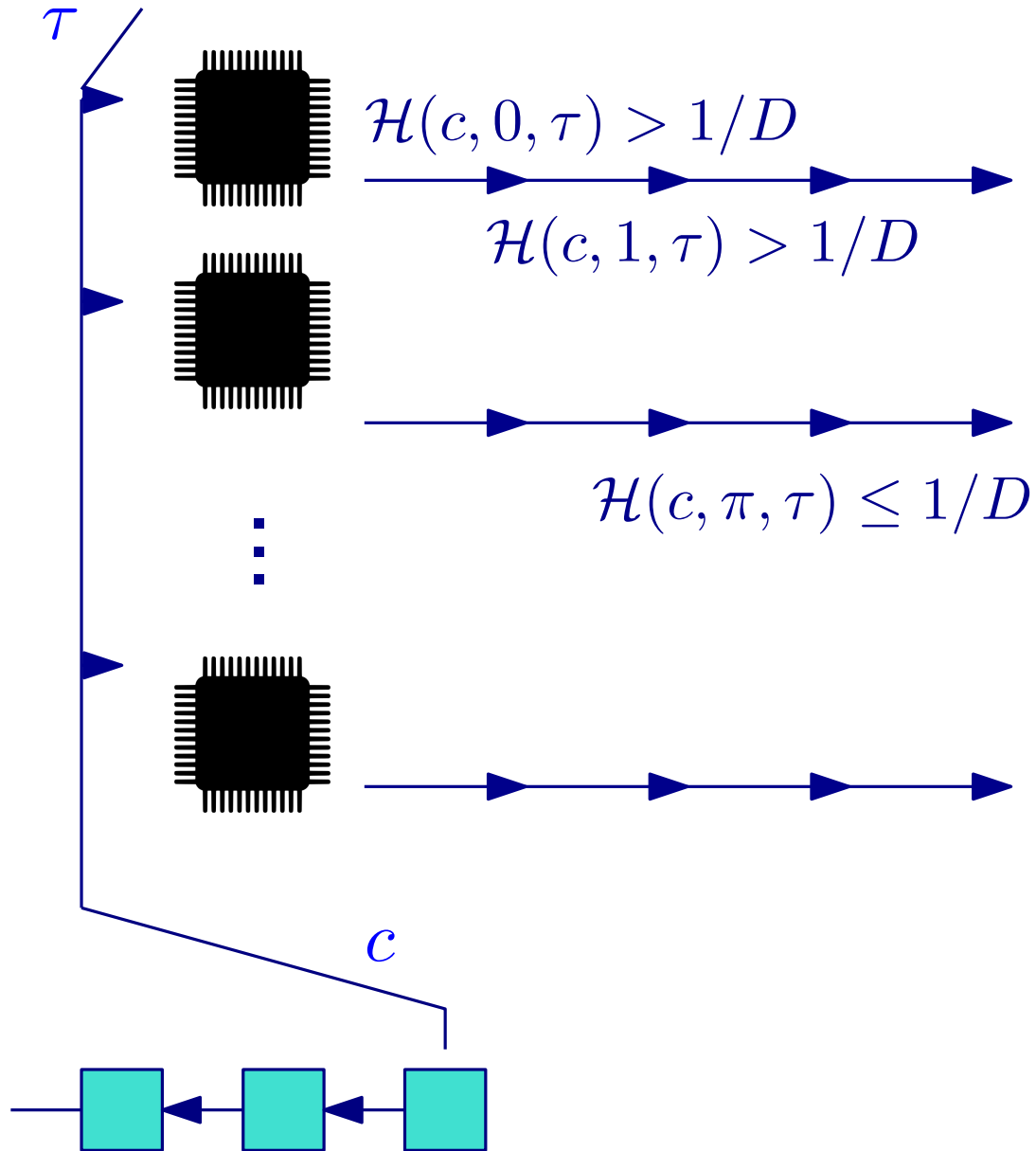
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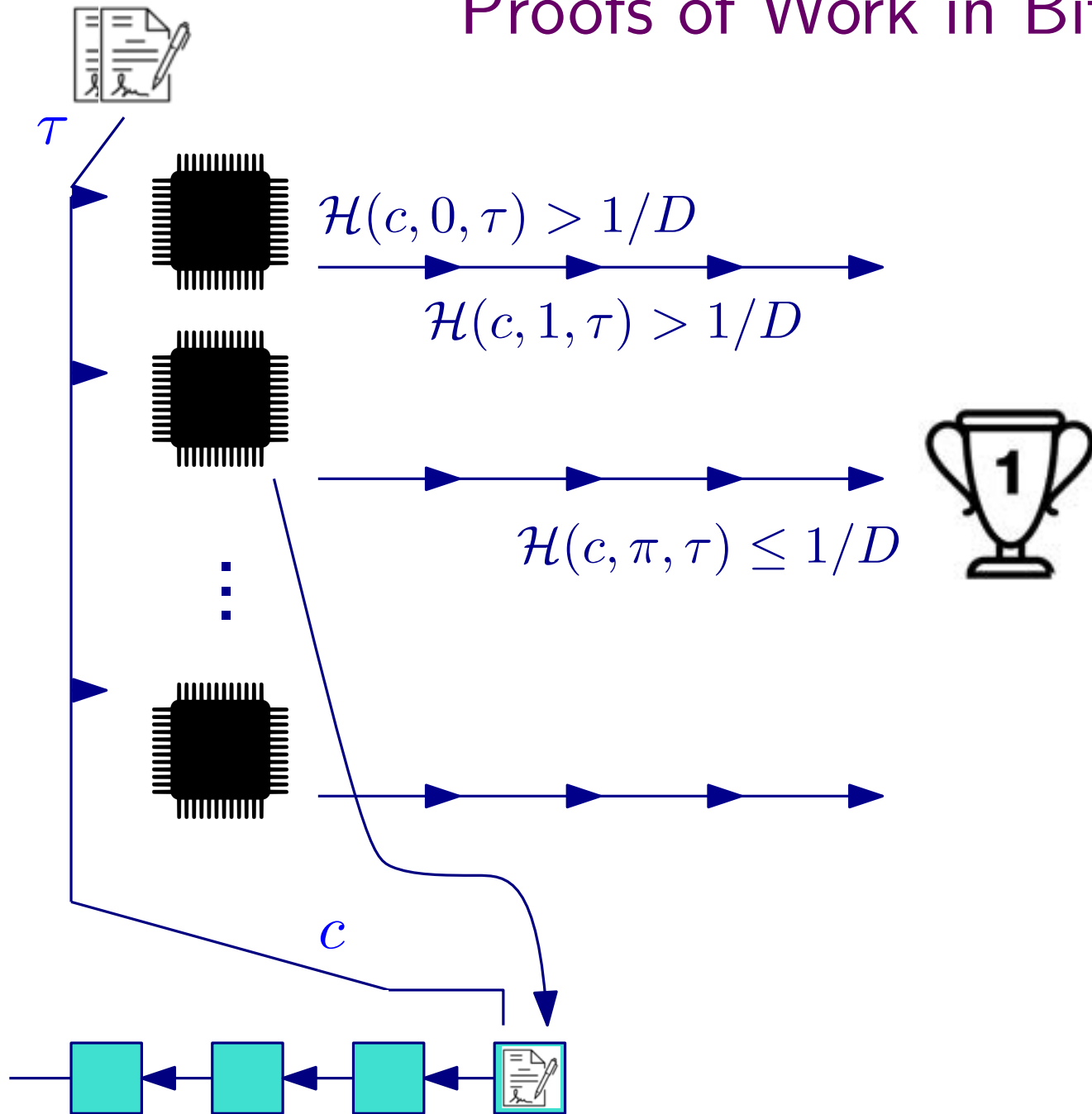
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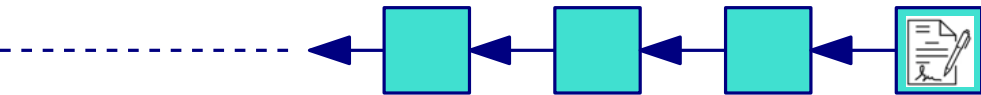
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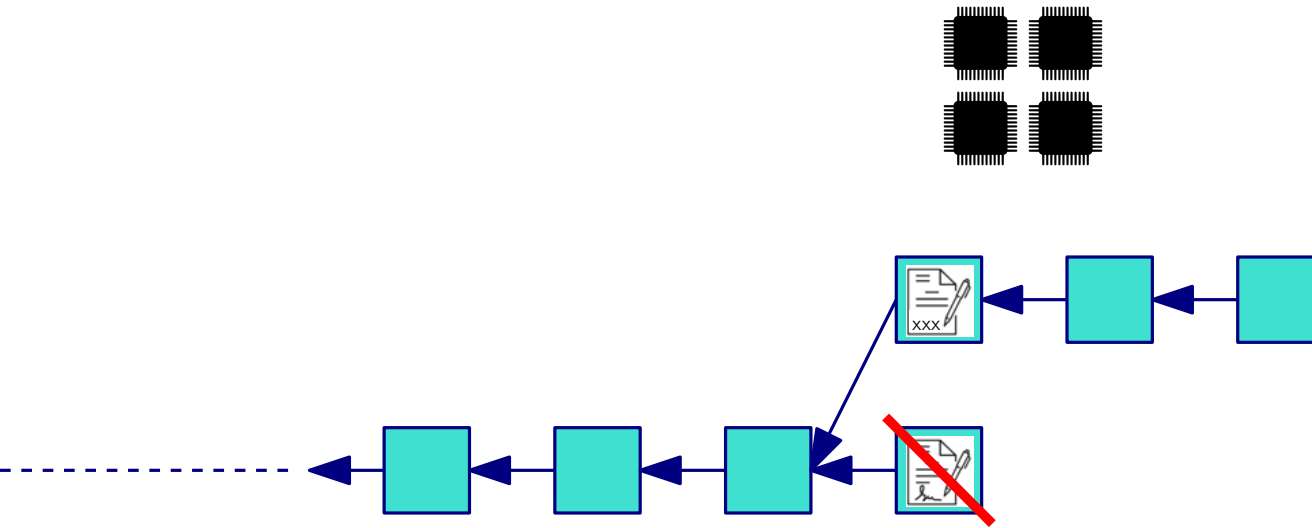
Proofs of Work in Bitcoin



Security of Bitcoin



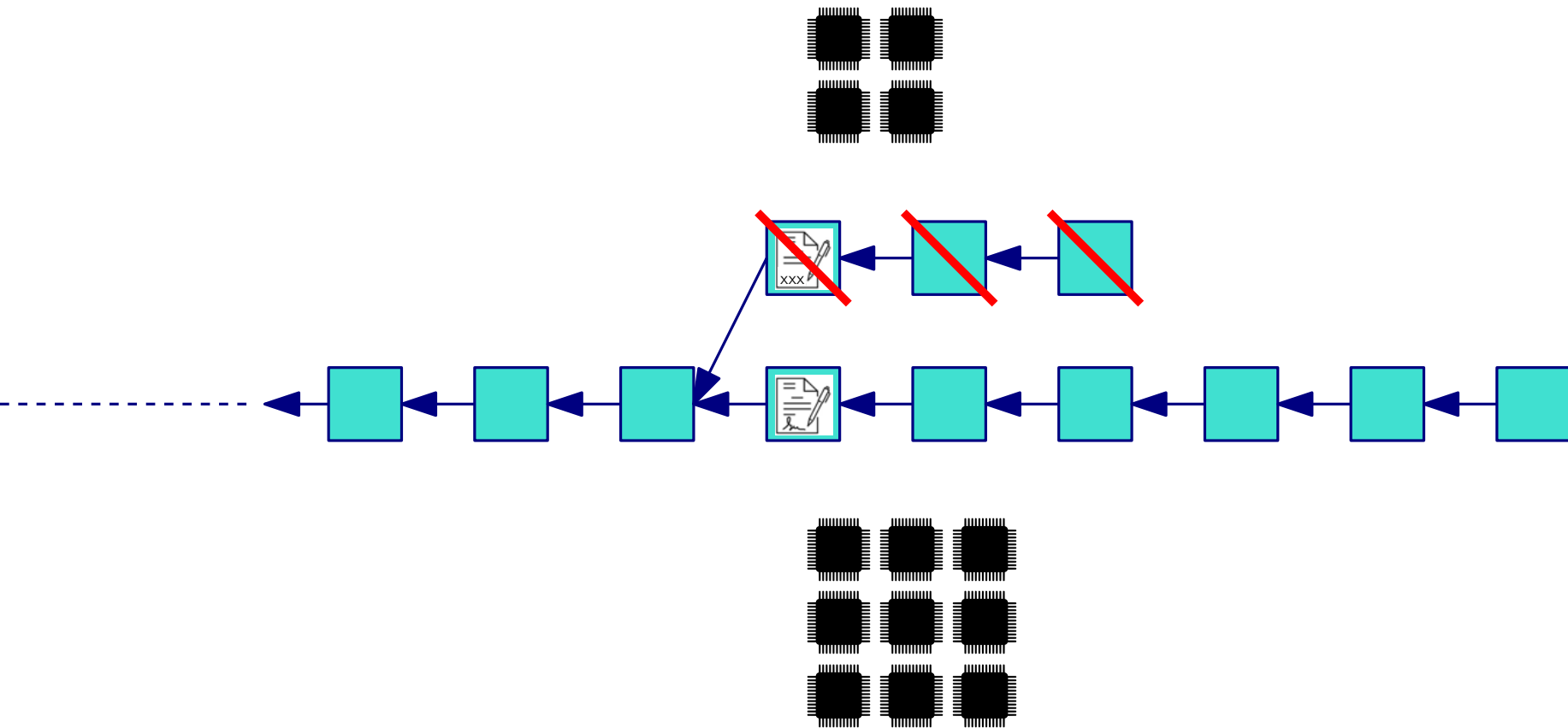
Security of Bitcoin



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Security of Bitcoin





PERMISSIONLESS BLOCKCHAIN

WHAT ARE PERMISSIONLESS BLOCKCHAINS?

Permissionless blockchains are blockchains that require no permission to join and interact with.

CHARACTERISTICS

- ⚡ Truly decentralized
- ⚡ Transparent network
- ⚡ Immutability



ADVANTAGES

- ⚡ Open to all
- ⚡ Brings trust to all users
- ⚡ Offers high security



DISADVANTAGES

- ⚡ Slow transaction speed
- ⚡ Harder to scale
- ⚡ Not energy efficient



USE CASES

- ⚡ Digital Identity
- ⚡ Voting
- ⚡ Fundraising



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- ⚡ Governance structure
- ⚡ Private transactions
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- ⚡ Food tracking
- ⚡ Banking and payments
- ⚡ Supply chain management



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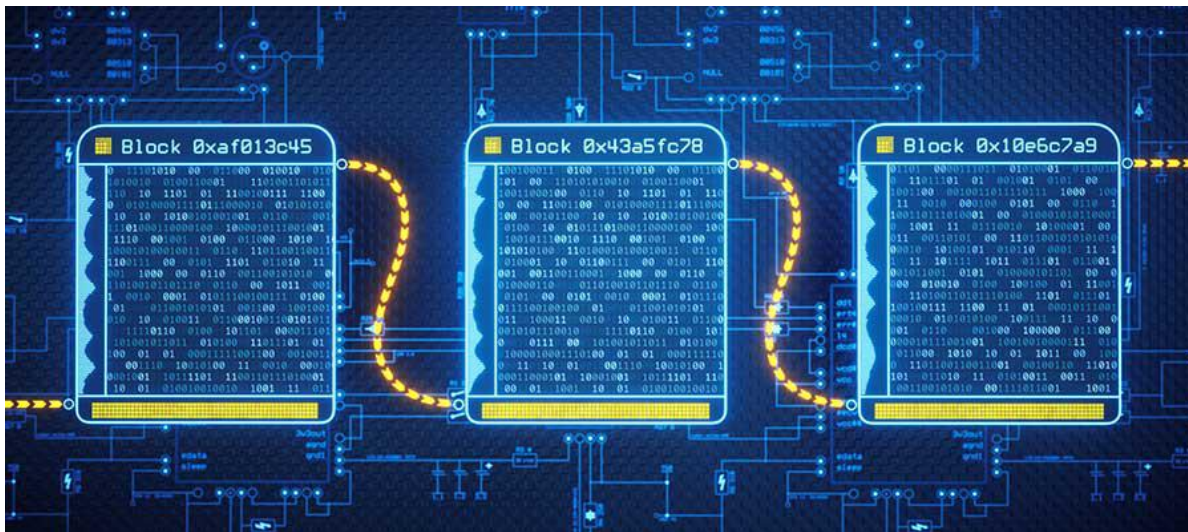


Consensus and Application Layer



Application layer

- UTXA/transactions (Bitcoin)
- Smart Contracts (Ethereum)



Consensus Layer

- Throughput
- Finality/Latency
- Proof of Work vs. Proof of Stake

BLOCKCHAIN SUSTAINABILITY



Environmental
Sustainability



Technological
Sustainability



Social
Sustainability



Economic
Sustainability

Energy/Hardware
waste of consensus

BLOCKCHAIN SUSTAINABILITY



Environmental Sustainability



Technological Sustainability



Social Sustainability



Economic Sustainability

Energy/Hardware
waste of consensus

- Scalability bottlenecks
- Postquantum security

BLOCKCHAIN SUSTAINABILITY



Environmental Sustainability



Technological Sustainability



Social Sustainability



Economic Sustainability

Energy/Hardware
waste of consensus

Concentration of
mining/staking
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BLOCKCHAIN SUSTAINABILITY



Environmental Sustainability



Technological Sustainability



Social Sustainability



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Energy/Hardware
waste of consensus

Concentration of
mining/staking
power

Block-rewards
security vs.
inflation

BLOCKCHAIN FOR SUSTAINABILITY



Carbon Credit
Trading



Supply Chain
Transparency



Renewable
Energy Certificates



Verifiable
Sustainability Claims

BLOCKCHAIN SUSTAINABILITY



Environmental
Sustainability



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Sustainability



Social
Sustainability



Economic
Sustainability

Scalability / Transactions per second

Cryptocurrencies Transaction Speeds Compared to Visa & Paypal

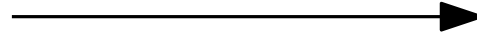
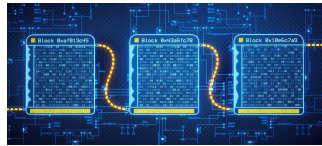


Article & Sources:

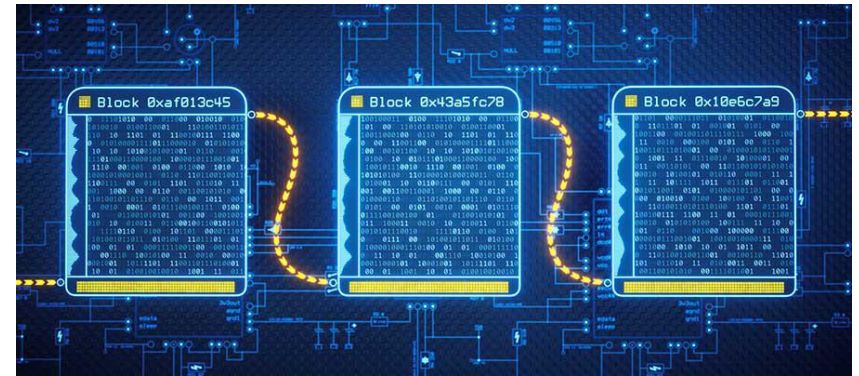
<https://howmuch.net/articles/crypto-transaction-speeds-compared>

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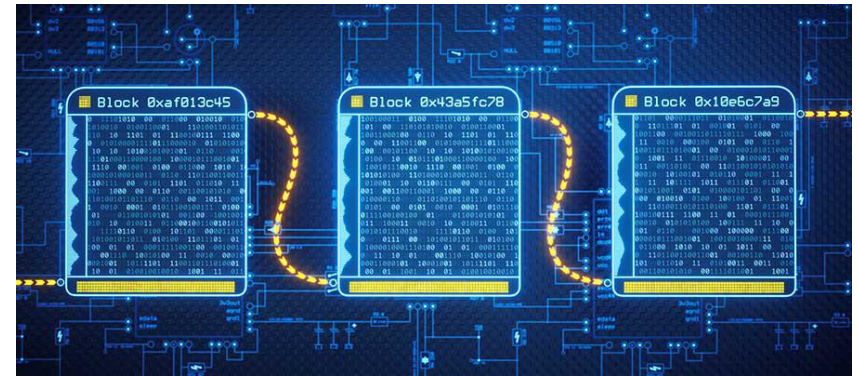
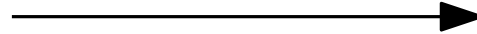
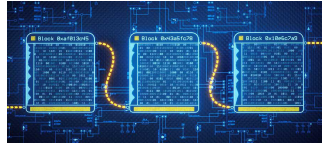
Scaling Blockchains



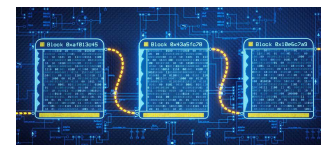
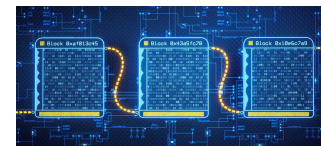
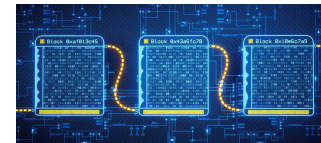
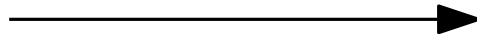
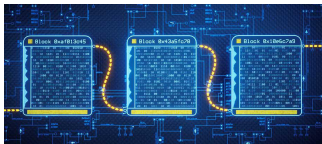
Increase block size and/or rate



Scaling Blockchains



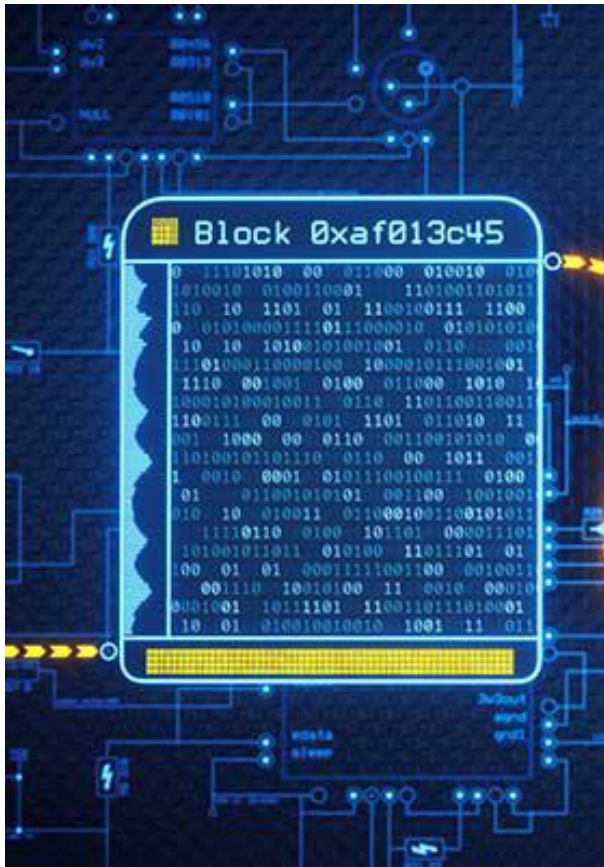
Increase block size and/or rate



Sharding

Scaling Blockchains

Layer 2 Solution: Rollups



crypto magic
ZK-SNARKs^a

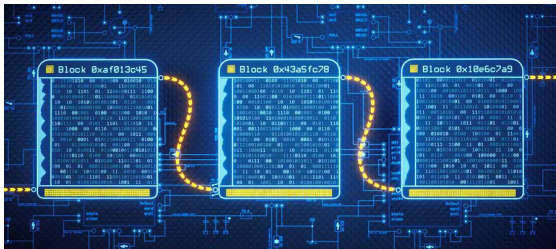
^aZero-Knowledge Succinct Non-Interactive
Argument of Knowledge

Scaling Blockchains

Layer 2 solution: Payment Networks



Payment network, e.g. Lightning



Layer 1: Blockchain, e.g. Bitcoin

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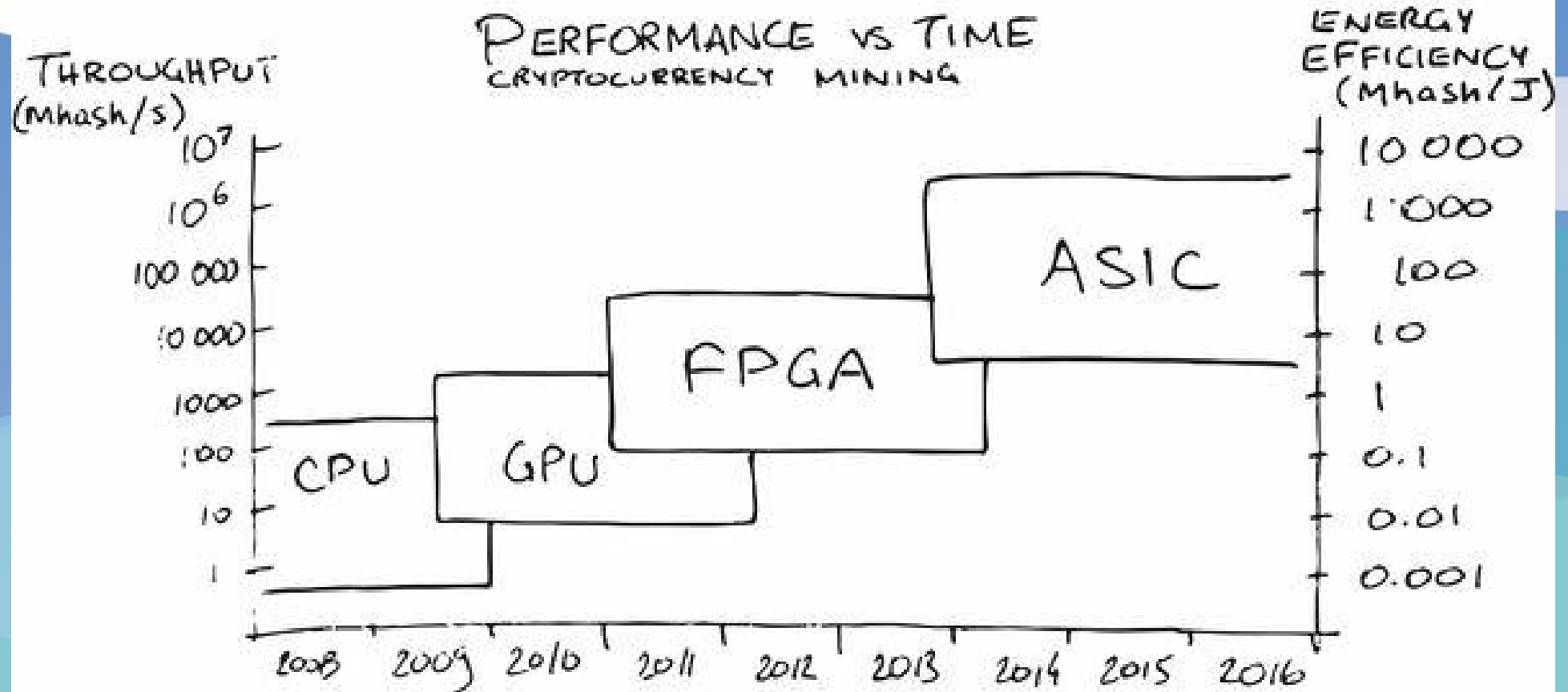
Bitcoin Mining

Nakamoto's vision: spare CPU cycles used for mining



Bitcoin Mining

Nakamoto's vision: spare CPU cycles used for mining



Bitcoin Mining



Bitcoin Sustainability

<https://digiconomist.net/bitcoin-energy-consumption>

Single Bitcoin Transaction Footprints

Carbon Footprint

462.90 kgCO₂



Equivalent to the carbon footprint of 1,025,937 VISA transactions or 77,149 hours of watching Youtube.

Electrical Energy

829.92 kWh



Equivalent to the power consumption of an average U.S. household over 28,45 days.

Electronic Waste

194.10 grams



Equivalent to the weight of 1.18 iPhones 12 or 0.40 iPads. (Find more info on e-waste [here](#).)

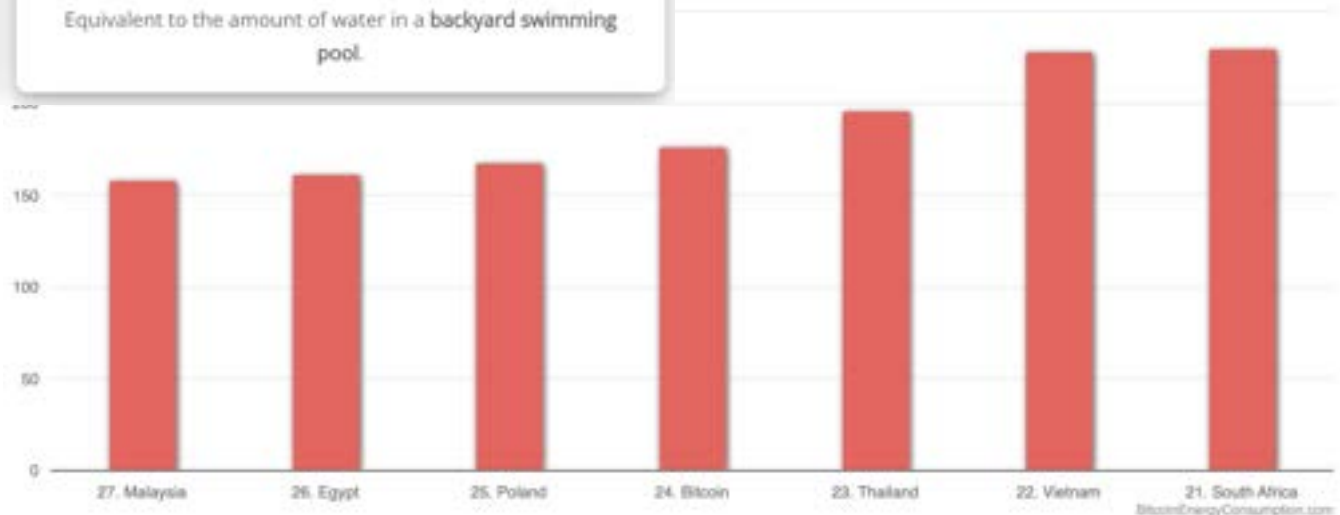
Fresh Water Consumption

13,080 liters



Equivalent to the amount of water in a backyard swimming pool.

ion by Country



Can we have a more sustainable
Blockchain?



Alternatives to Proof of Work Mining?



Proofs of (Useful) Work

(Bitcoin, old Ethereum, Primecoin...)
mining resource: work

Alternatives to Proof of Work Mining?



Proofs of (Useful) Work

(Bitcoin, old Ethereum, Primecoin...)
mining resource: work



Proofs of Stake

(Ethereum, Algorand,
Ourboros,...)

mining resource: (staked) coins

Alternatives to Proof of Work Mining?

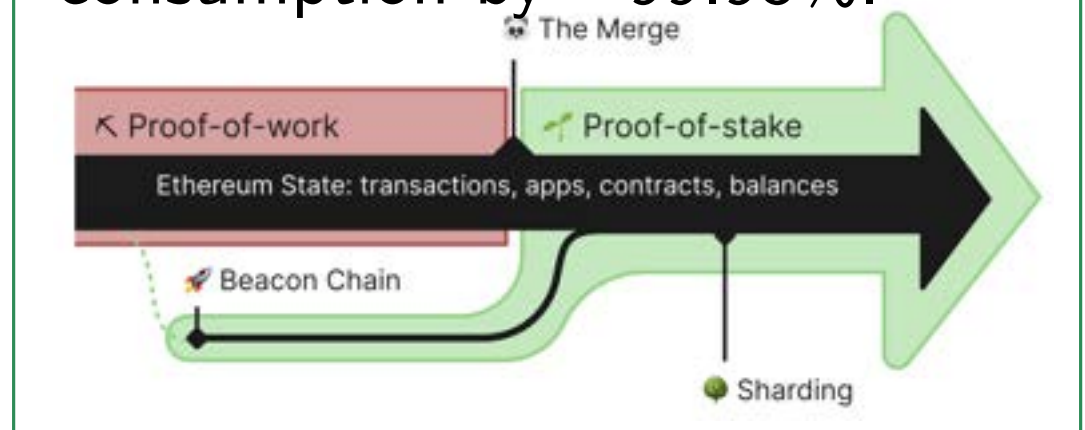


Proofs of (Useful) Work

(Bitcoin, old Ethereum, Primecoin...)

mining resource: work

September 2022, “the Merge” reduced Ethereum’s energy consumption by $\approx 99.95\%$.



Proofs of Stake

(Ethereum, Algorand, Ourboros,...)

mining resource: (staked) coins

Proof of Stake Issues

NOTHING-AT-STAKE



LONG-RANGE ATTACKS



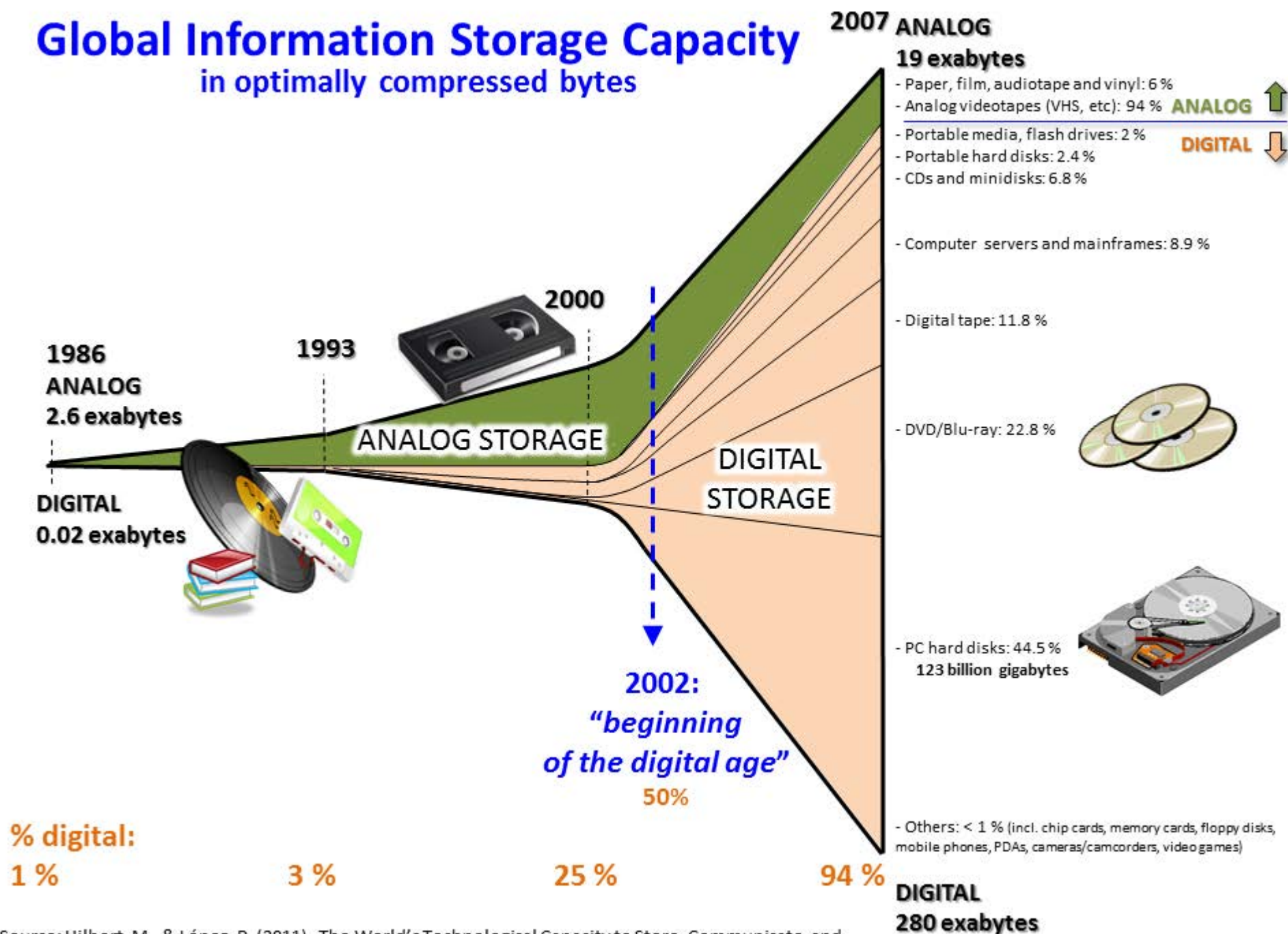
WEALTH CONCENTRATION



CENTRALIZATION



Global Information Storage Capacity in optimally compressed bytes



Work vs. Space vs. Stake Mining/Farming



Work vs. Space vs. Stake Mining/Farming



Resource is



External



External



Internal

Work vs. Space vs. Stake Mining/Farming



Resource is Power consumption



External

Huge



External

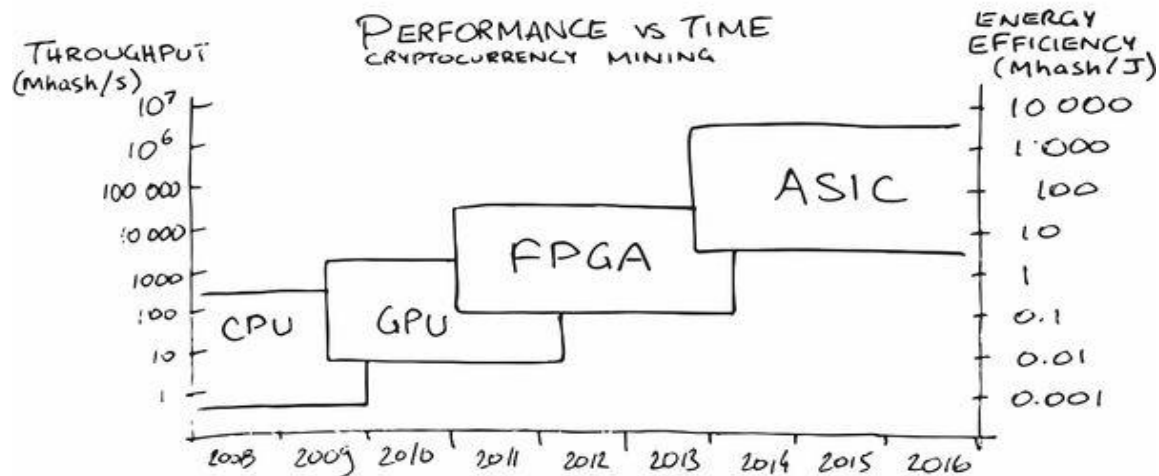
Tiny



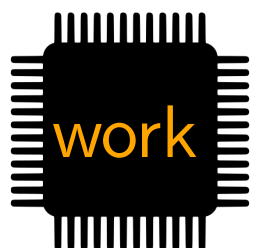
Internal

Tiny

Work vs. Space vs. Stake Mining/Farming



Resource is Power consumption Hardware



External

Huge

Application Specific
Integrated Circuits
(ASIC)



External

Tiny

General Purpose Disk
Storage



Internal

Tiny

None

Proofs of Space [DFKP'15]



Proofs of Space [DFKP'15]



73735	45963	78134	63873
02965	58303	90708	20025
98859	23851	27965	62394
33666	62570	64775	78428
81666	26440	20422	05720

15838	47174	76866	14330
89793	34378	08730	56522
78155	22466	81978	57323
16381	66207	11698	99314
75002	80827	53867	37797

99982	27601	62686	44711
84543	87442	50033	14021
77757	54043	46176	42391
80871	32792	87989	72248
30500	28220	12444	71840

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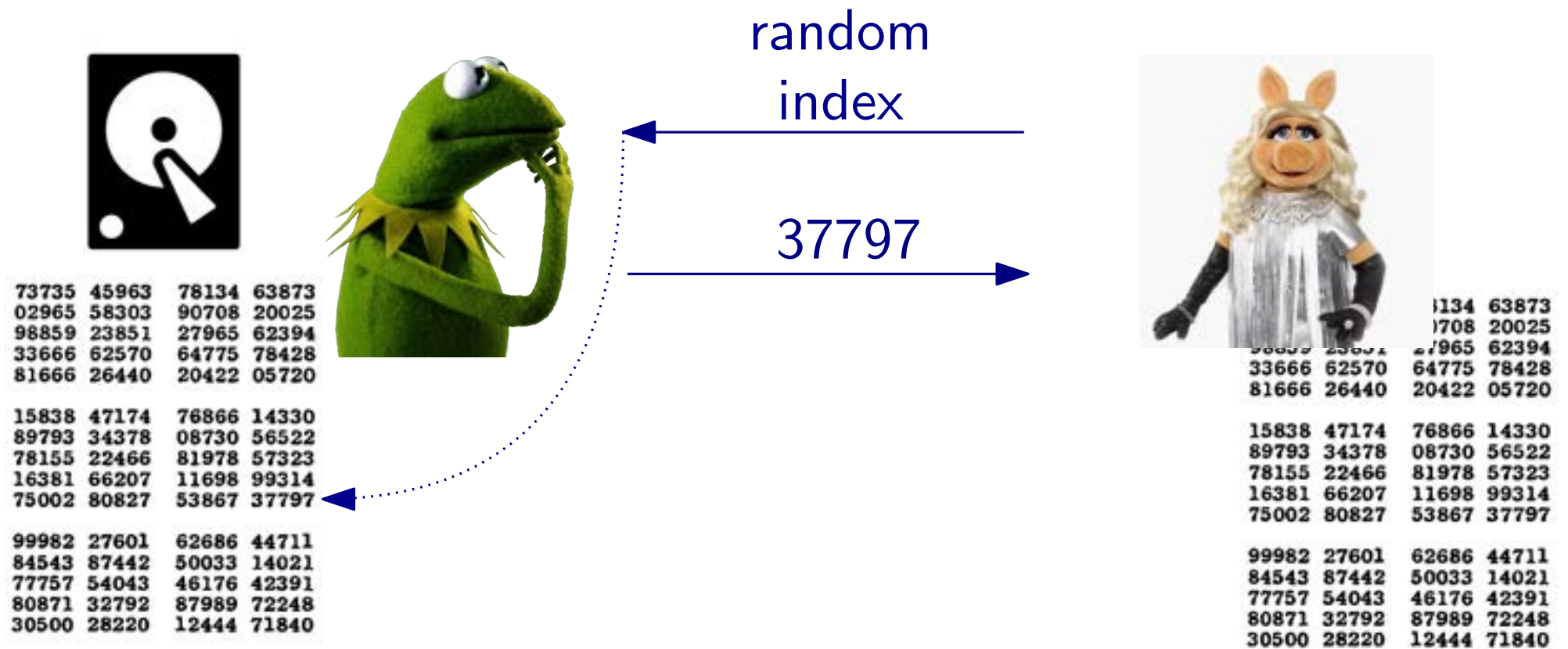


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Proofs of Space [DFKP'15]



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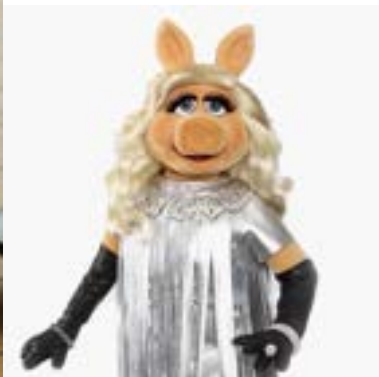
73735	45963	78134	63873
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TOO MUCH
COMMUNICATION

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Proofs of Space [DFKP'15]

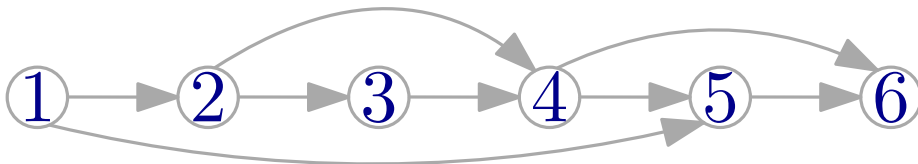


Stefan Dziembowski, Sebastian Faust, Vladimir Kolmogorov, Krzysztof Pietrzak: Proofs of Space. CRYPTO 2015

Proofs of Space [DFKP'15]



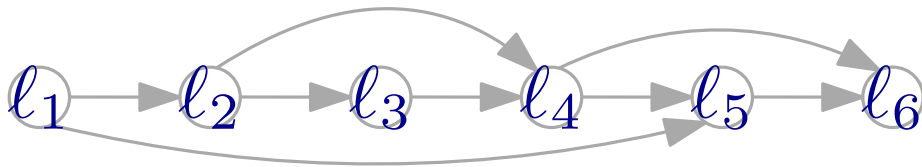
<https://www.pebbling-game.at/>



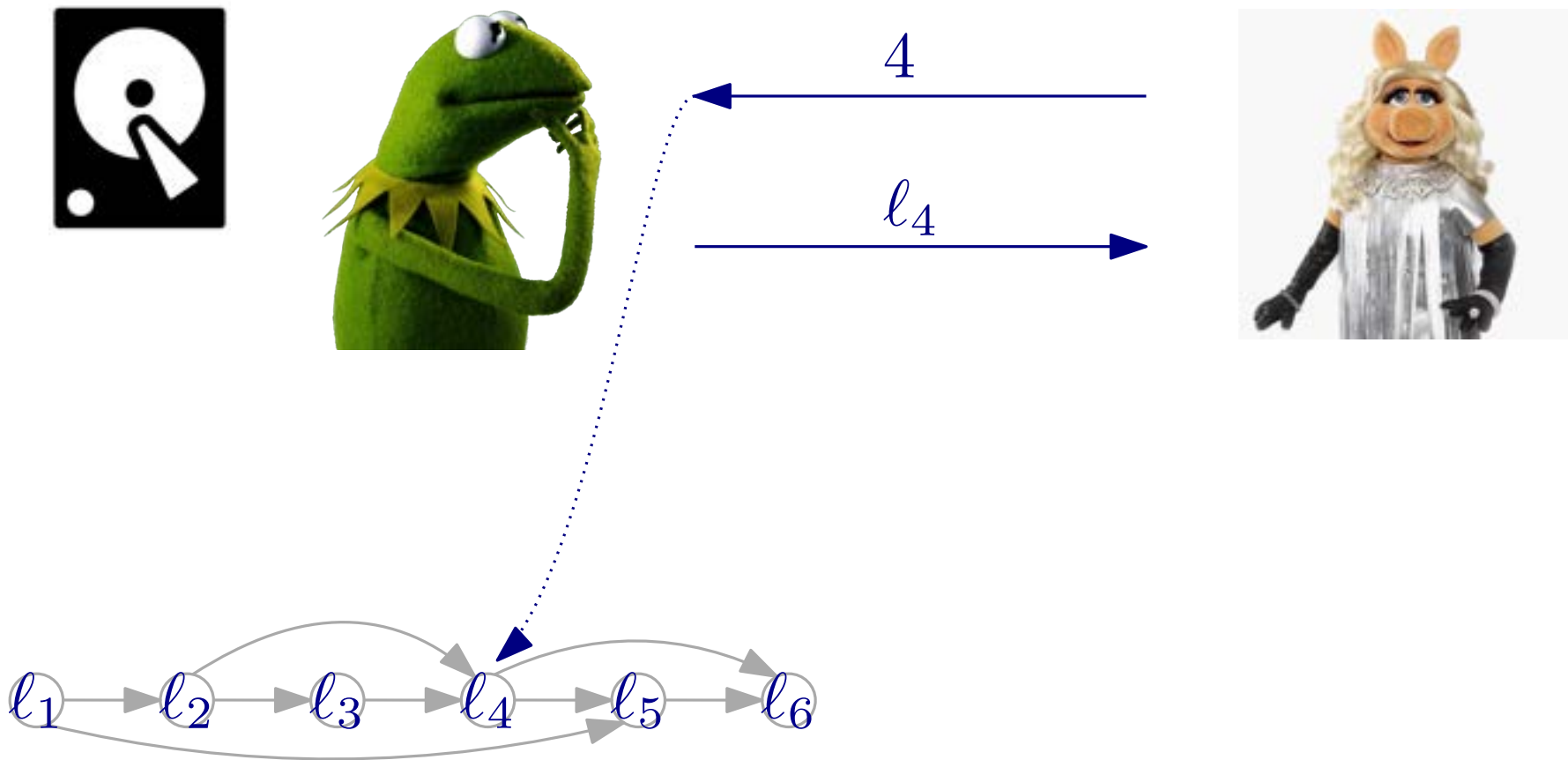
Proofs of Space [DFKP'15]



$$\ell_4 := \text{hash}(\ell_2, \ell_3)$$



Proofs of Space [DFKP'15]



Sustainable Blockchains at ISTA

PROOF OF SPACE



VERIFIABLE DELAY FUNCTIONS



Sustainable Blockchains at ISTA



The Guardian, May 26, 2021

New cryptocurrency Chia blamed for hard drive shortages

Speculators buy up vital components as demand surges for rival to bitcoin that requires huge storage space



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Driving the circular economy for storage

The Circular Drive Initiative (CDI) is a partnership of global leaders in digital storage, data centers, sustainability, and blockchain collaborating to reduce e-waste by enabling, driving, and promoting the secure reuse of storage hardware.



BLOCKCHAIN SUSTAINABILITY



Environmental
Sustainability



Technological
Sustainability

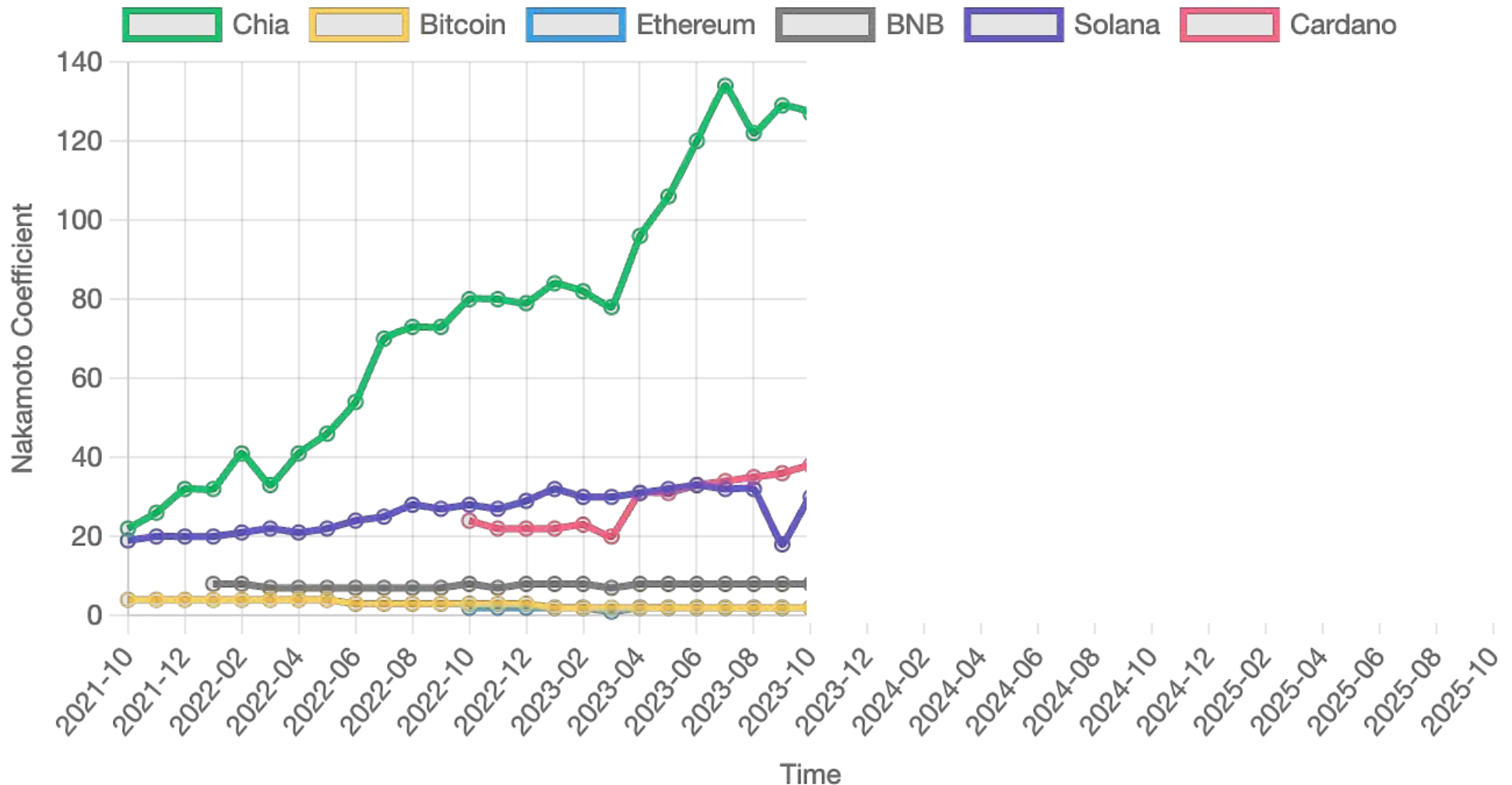


Social
Sustainability



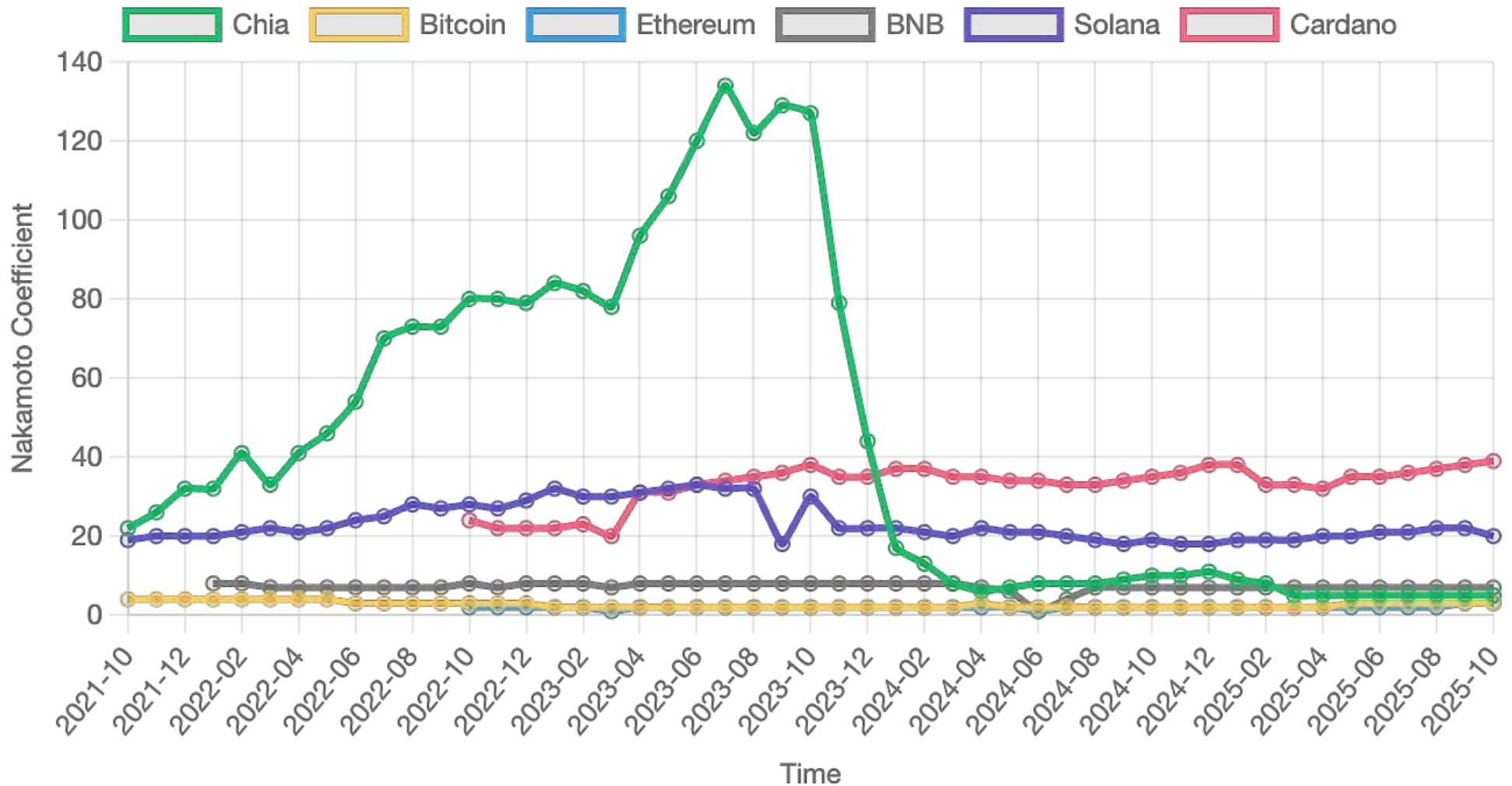
Economic
Sustainability

The **Nakamoto coefficient** is the minimum number of entities (e.g., miners, validators, or nodes) that together control enough of the system to disrupt consensus or compromise its integrity.



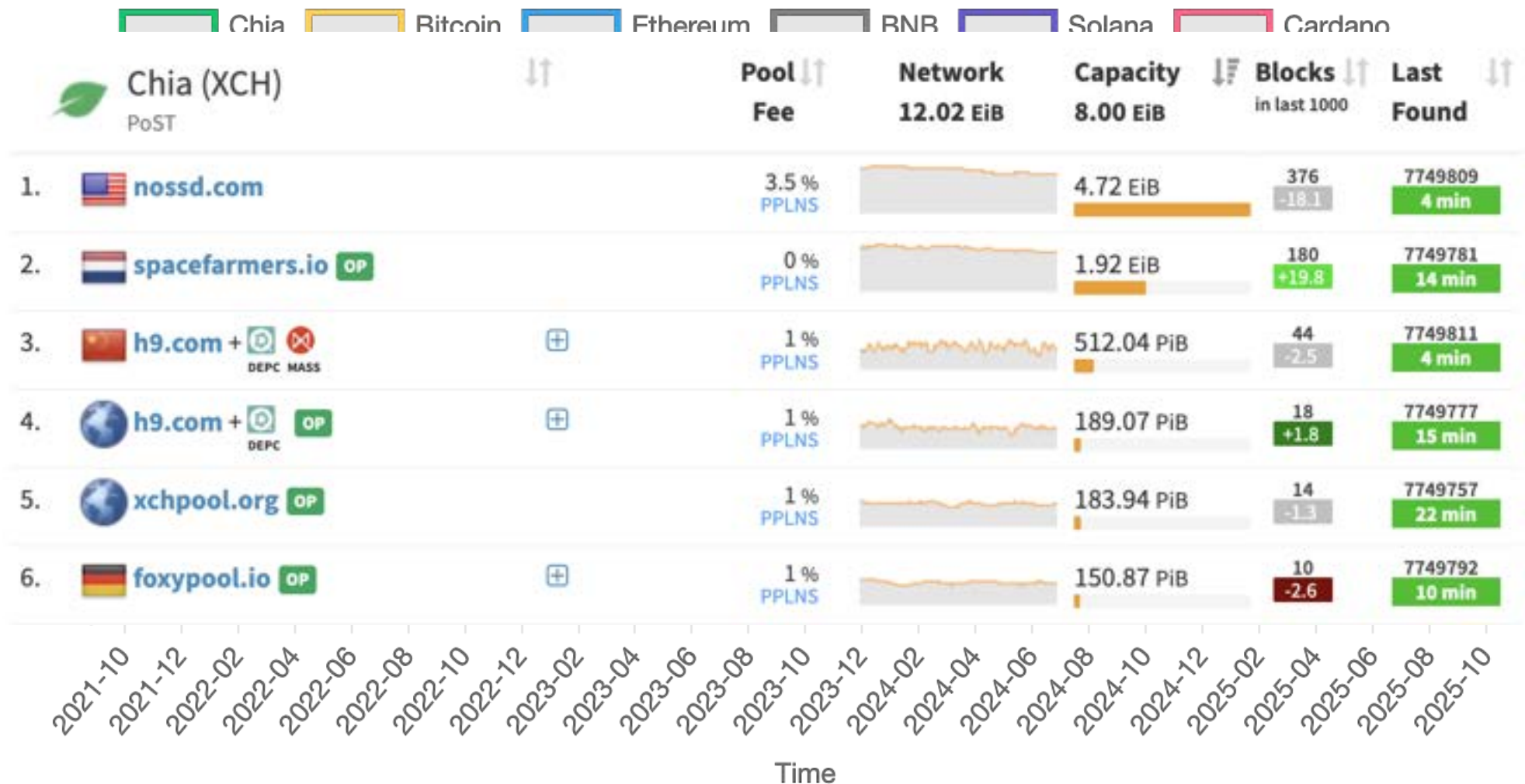
<https://xch.farm/decentralization/>

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<https://xch.farm/decentralization/>

BLOCKCHAIN FOR SUSTAINABILITY



Carbon Credit
Trading



Supply Chain
Transparency



Renewable
Energy Certificates



Verifiable
Sustainability Claims

<https://www.youtube.com/watch?v=cXwTV2bAnvl>

World Bank Group

Climate Warehouse

A Global Public Data-Layer for Carbon Markets



0:04 / 5:08



BLOCKCHAIN FOR SUSTAINABILITY



Carbon Credit
Trading



Supply Chain
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Verifiable
Sustainability Claims

DePIN